STAT679 Computing for Data Science and Statistics

Lecture 4: Dictionaries and Tuples

Two more fundamental built-in data structures

Dictionaries

Python dictionaries generalize lists

Allow indexing by arbitrary immutable objects rather than integers

Fast lookup and retrieval

https://docs.python.org/3/tutorial/datastructures.html#dictionaries

Tuples

Similar to a list, in that it is a sequence of values

But unlike lists, tuples are immutable

https://docs.python.org/3/tutorial/datastructures.html#tuples-and-sequences

Generalized lists: Python dict()

Python dictionary generalizes lists

list(): indexed by integers

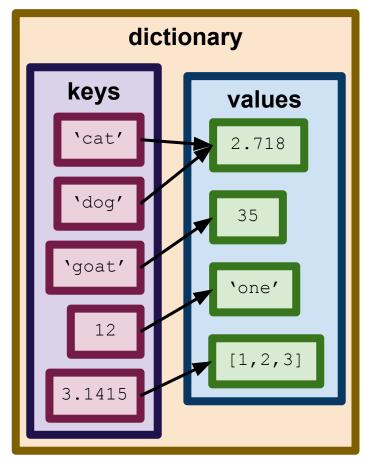
dict(): indexed by (almost) any data type

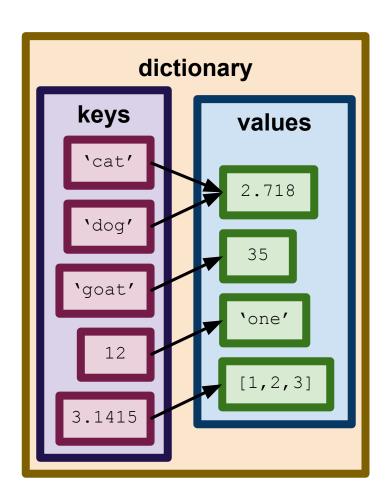
Dictionary contains:

a set of indices, called keys

A set of values (called **values**, shockingly)

Each key associated with one (and only one) value
 key-value pairs, sometimes called items
 Like a function f: keys -> values



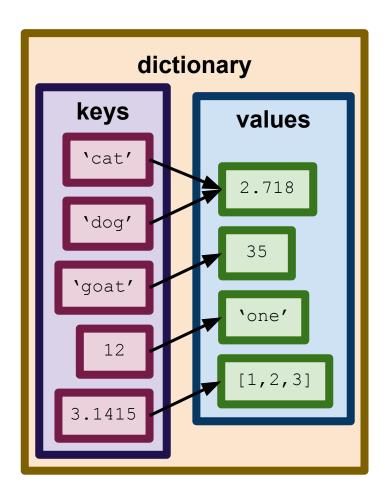


Dictionary maps keys to values.

E.g., 'cat' mapped to the float 2.718

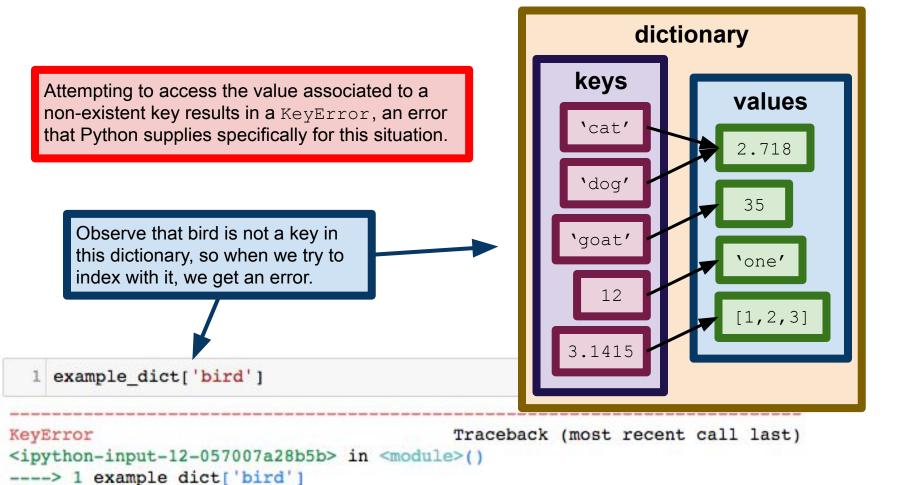
Of course, the dictionary at the left is kind of silly. In practice, keys are often all of the same type, because they all represent a similar kind of object

Example: might use a dictionary to map UMich unique names to people



```
example dict['cat']
2.718
    example_dict['dog']
2.718
    example dict['goat']
35
    example dict[12]
'one'
    example dict[3.1415]
[1, 2, 3]
```

Access the value associated to key x by dictionary[x].



KeyError: 'bird'

Example: University of Mishuges IT wants to store the correspondence between the usernames (UM IDs) of students to their actual names. A dictionary is a very natural data structure for this.

```
umid2name = dict()
   umid2name['aeinstein'] = 'Albert Einstein'
 3 umid2name['kyfan'] = 'Ky Fan'
   umid2name['enoether'] = 'Emmy Noether'
 5 umid2name['cshannon'] = 'Claude Shannon'
   umid2name['cshannon']
'Claude Shannon'
   umid2name['enoether']
'Emmy Noether'
   umid2name['enoether'] = 'Amalie Emmy Noether'
 2 umid2name['enoether']
'Amalie Emmy Noether'
```

Create an empty dictionary (i.e., a dictionary with no key-value pairs stored in it. This should look familiar, since it is very similar to list creation.

```
umid2name = dict()
    umidzname | deinstein' ] = 'Albert Einstein'
   umid2name['kyfan'] = 'Ky Fan'
   umid2name['enoether'] = 'Emmy Noether'
   umid2name['cshannon'] = 'Claude Shannon'
   umid2name['cshannon']
'Claude Shannon'
   umid2name['enoether']
'Emmy Noether'
   umid2name['enoether'] = 'Amalie Emmy Noether'
   umid2name['enoether']
'Amalie Emmy Noether'
```

Populate the dictionary. We are adding four key-value pairs, corresponding to four users in the system.

```
umid2name['aeinstein'] = 'Albert Einstein
    umid2name['kyfan'] = 'Ky Fan'
    umid2name['enoether'] = 'Emmy Noether'
   umid2name['cshannon'] = 'Claude Shannon'
   umid2name['cshannon']
'Claude Shannon'
   umid2name['enoether']
'Emmy Noether'
   umid2name['enoether'] = 'Amalie Emmy Noether'
   umid2name['enoether']
'Amalie Emmy Noether'
```

```
umid2name = dict()
   umid2name['aeinstein'] = 'Albert Einstein'
 3 umid2name['kyfan'] = 'Ky Fan'
   umid2name['enoether'] = 'Emmy Noether'
 5 umid2name['cshannon'] = 'Claude Shannon'
   umid2name['cshannon']
Claude Shannon'
   umid2name['enoether']
Emmy Noether'
   umid2name['enoether'] = 'Amalie Emmy Noether'
   umid2name['enoether']
```

'Amalie Emmy Noether'

Retrieve the value associated with a key. This is called **lookup**.

```
1 umid2name = dict()
2 umid2name['aeinstein'] = 'Albert Einstein'
3 umid2name['kyfan'] = 'Ky Fan'
4 umid2name['enoether'] = 'Emmy Noether'
5 umid2name['cshannon'] = 'Claude Shannon'
1 umid2name['cshannon']
```

Emmy Noether's actual legal name was Amalie Emmy Noether, so we have to update her record. Note that updating is syntactically the same as initial population of the dictionary.

```
1 umid2name['enoether']
'Emmy Noether'

1 umid2name['enoether'] = 'Amalie Emmy Noether
2 umid2name['enoether']

Amalie Emmy Noether'
```

Displaying Items

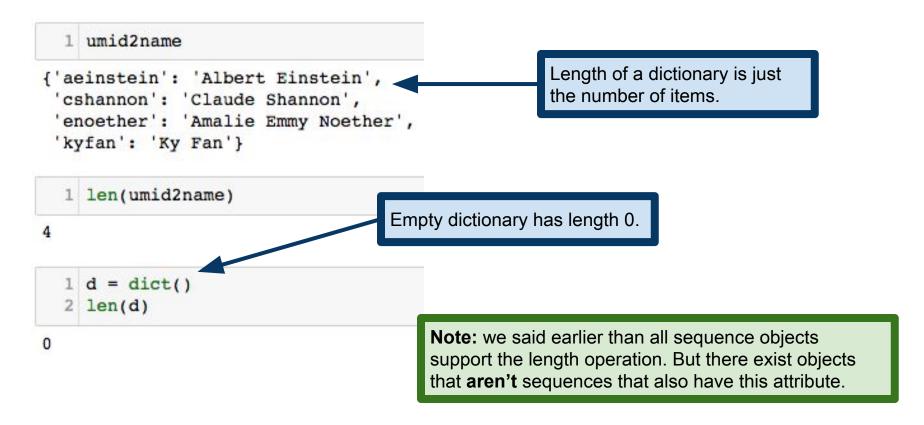
'Ky Fan'

Printing a dictionary lists its **items** (key-value pairs), in this rather odd format...

are stored in memory. More on this soon.

```
1 example dict
{3.1415: [1, 2, 3], 12: 'one', 'cat': 2.718, 'dog': 2.718, 'goat': 35}
  1 umid2name
                                                               ...but we can use that format
{ 'aeinstein': 'Albert Einstein',
                                                               to create a new dictionary.
 'cshannon': 'Claude Shannon',
 'enoether': 'Amalie Emmy Noether',
 'kyfan': 'Ky Fan'}
  1 umid2name = {'aeinstein': 'Albert Einstein',
  2 'cshannon': 'Claude Shannon',
  3 'enoether': 'Amalie Emmy Noether',
    'kyfan': 'Ky Fan')
                                                     Note: the order in which items are printed
                                                     isn't always the same, and (usually) isn't
  1 umid2name['kyfan']
                                                     predictable. This is due to how dictionaries
```

Dictionaries have a length



Checking set membership

```
1 umid2name
{'aeinstein': 'Albert Einstein',
   'cshannon': 'Claude Shannon',
   'enoether': 'Amalie Emmy Noether',
   'kyfan': 'Ky Fan'}
```

Suppose a new student, Andrey Kolmogorov is enrolling at UMish. We need to give him a unique name, but we want to make sure we aren't assigning a name that's already taken.

1 'akolmogorov' in umid2name
False

1 'enoether' in umid2name

Dictionaries support checking whether or not an element is present **as a key**, similar to how lists support checking whether or not an element is present in the list.

True

```
from random import randint
listlen = 1000000
list_of_numbers = listlen*[0]
dict_of_numbers = dict()
for i in range(listlen):
    n = randint(10000000,99999999)
list_of_numbers[i] = n
dict_of_numbers[n] = 1
```

```
1 8675309 in list_of_numbers
```

False

```
1 1240893 in list_of_numbers
```

True

```
1 8675309 in dict_of_numbers
```

False

```
1 1240893 in dict_of_numbers
```

True

Lists and dictionaries provide our first example of how certain **data structures** are better for certain tasks than others.

Example: I have a large collection of phone numbers, and I need to check whether or not a given number appears in the collection. Both dictionaries and lists support **membership checks** of this sort, but it turns out that dictionaries are much better suited to the job.

```
from random import randint
listlen = 1000000
list_of_numbers = listlen*[0]
dict_of_numbers = dict()
for i in range(listlen):
    n = randint(1000000,9999999)
list_of_numbers[i] = n
dict_of_numbers[n] = 1
```

```
This block of code generates 1000000 random "phone numbers", and creates (1) a list of all the numbers and (2) a dictionary whose keys are all the numbers.
```

```
1 8675309 in list_of_numbers
```

False

```
1 1240893 in list_of_numbers
```

True

```
1 8675309 in dict_of_numbers
```

False

```
1 1240893 in dict_of_numbers
```

True

```
from random import randint
listler = 1000000

listler = 1000000

listler = 1000000

list_of_numbers = listlen*[0]

dict_of_numbers = dict()

for i in range(listlen):

n = randint(10000000,99999999)

list_of_numbers[i] = n

dict_of_numbers[n] = 1
```

```
1 8675309 in list_of_numbers
```

False

```
1 1240893 in list_of_numbers
```

True

```
1 8675309 in dict_of_numbers
```

False

```
1 1240893 in dict_of_numbers
```

True

The random module supports a bunch of random number generation operations. We'll see more on this later in the course. https://docs.python.org/3/library/random.html

```
from random import randint
   listlen = 1000000
    list of numbers = listlen*[0]
                                                      Initialize a list (of all zeros) and
    dict of numbers = dict()
                                                      an empty dictionary.
        n = randint(1000000,99999999)
        list of numbers[i] = n
        dict of numbers[n] = 1
  1 8675309 in list of numbers
False
  1 1240893 in list of numbers
True
  1 8675309 in dict_of_numbers
False
  1 1240893 in dict of numbers
```

True

```
1 from random import randint
  2 \text{ listlen} = 10000000
  3 list of numbers = listlen*[0]
   for i in range(listlen):
                                                    Generate listlen random numbers, writing
        n = randint(1000000,99999999)
        list of numbers[i] = n
                                                    them to both the list and the dictionary.
        dict of numbers[n] = 1
  1 8675309 in list of numbers
False
  1 1240893 in list of numbers
True
  1 8675309 in dict of numbers
False
  1 1240893 in dict of numbers
```

True

```
1 from random import randint
  2 listlen = 1000000
    list of numbers = listlen*[0]
    dict of numbers = dict()
    for i in range(listlen):
        n = randint(1000000,99999999)
        list of numbers[i] = n
        dict of numbers[n] = 1
  1 8675309 in list_of_numbers
False
                                                  This is slow.
  1 1240893 in list of numbers
True
  1 8675309 in dict_of_numbers
False
                                                  This is fast.
  1 1240893 in dict of numbers
True
```

```
import time
   8675309 in list of nabers
    time.time() - start time
0.10922789573669434
  1 start time = time.time()
  2 8675309 in dict of numbers
  3 time.time() - start time
```

0.0002219676971435547

Let's get a more quantitative look at the speed difference between lists and dictionaries.

The time module supports accessing the system clock, timing functions, and related operations. https://docs.python.org/3/library/time.html
Timing parts of your program to find where performance can be improved is called **profiling** your code. Python provides some built-in tools for more profiling, which we'll discuss later in the course, if time allows.

https://docs.python.org/3/library/profile.html

```
2 start_time = time.time()
3 8675309 in list_of_numbers
4 time.time() - start_time
0.10922789573669434
```

```
1 start_time = time.time()
2 8675309 in dict_of_numbers
3 time.time() - start_time
```

0.0002219676971435547

To see how long an operation takes, look at what time it is, perform the operation, and then look at what time it is again. The time difference is how long it took to perform the operation.

Warning: this can be influenced by other processes running on your computer. See documentation for ways to mitigate that inaccuracy.

```
import time
start_time = time.time()
3 8675309 in list_of_numbers
4 time.time() - start_time
0.10922789573669434
```

```
1 start_time = time.time()
2 8675309 in dict_of_numbers
3 time.time() - start_time
```

0.0002219676971435547

Checking membership in the dictionary is orders of magnitude faster! Why should that be?

```
1 import time
2 start_time = time.time()
3 8675309 in list_of_numbers
4 time.time() - start_time

0.10922789573669434
```

```
1 start_time = time.time()
2 8675309 in dict_of_numbers
3 time.time() - start_time
```

0.0002219676971435547

The time difference is due to how the in operation is implemented for lists and dictionaries.

Python compares x against each element in the list until it finds a match or hits the end of the list. So this takes time **linear** in the length of the list.

Python uses a **hash table**. This lets us check if x is in the dictionary in (almost) the same amount of time, regardless of how many items are in the dictionary. How is that possible?

Universe of objects







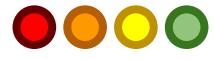






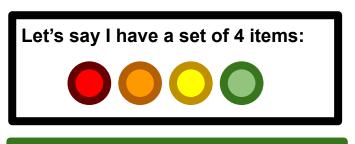


Let's say I have a set of 4 items:



I want to find a way to know **quickly** whether or not an item is in this set.

Universe of objects



I want to find a way to know **quickly** whether or not an item is in this set.

Hash function **f** maps objects to "buckets" (in this example, let's say there are four buckets)

 $f: \{ \color{red} \color{$

Hash function **f** maps objects to "buckets"

















Let's say I have a set of 4 items:



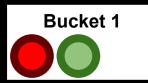
Assign objects to buckets based on the outputs of the hash function.



$$f(\bigcirc)=3$$

$$f(\bigcirc)=2$$

$$f(\bigcirc) = 1$$



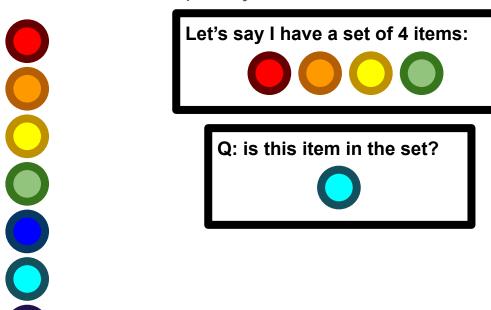


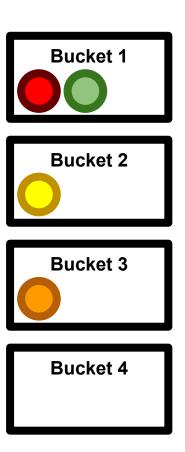


Bucket 3

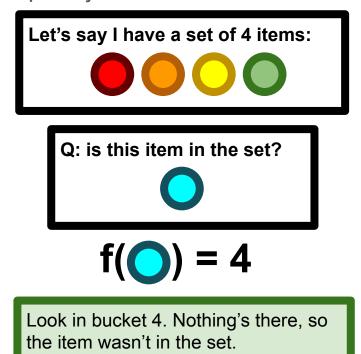


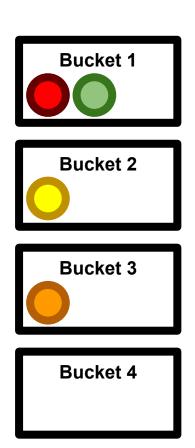
Bucket 4

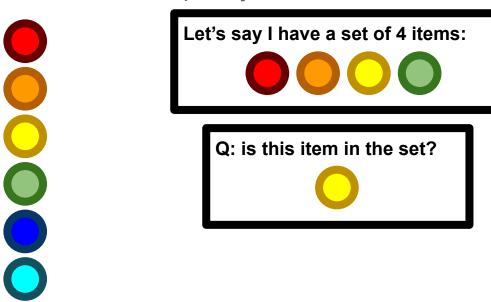


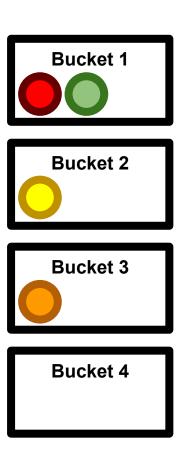




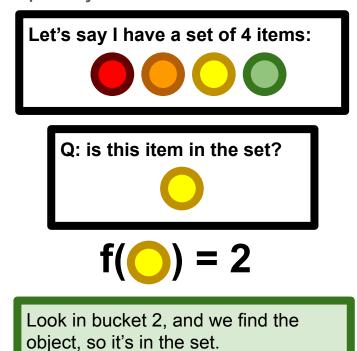


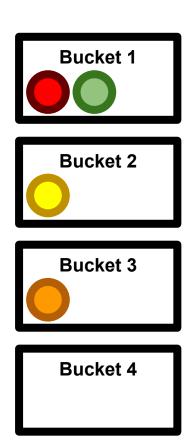


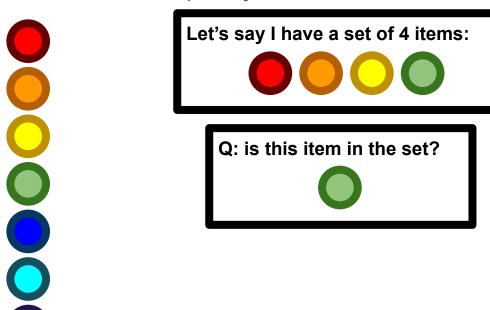


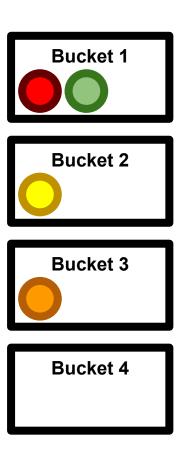








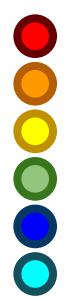


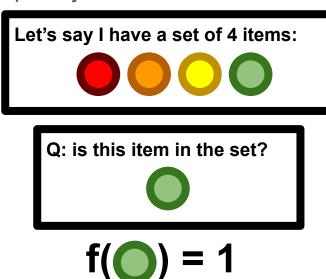


When more than one object falls in the same bucket, we call it a **hash collision**.

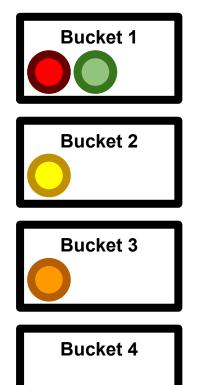
Crash course: hash tables

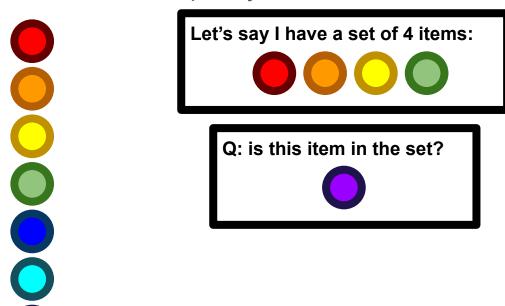
Hash function maps objects to "buckets"

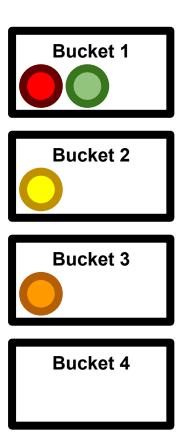




Look in bucket 1, and there's more than one thing. Compare against each of them, eventually find a match.







Worst possible case: have to check everything in the bucket only to conclude there's no match.

Crash course: hash tables

Hash function maps objects to "buckets"



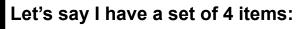












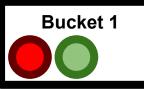


Q: is this item in the set?

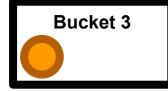


$$f(\bigcirc)=1$$

Look in bucket 1, and there's more than one thing. Compare against each of them, no match, so it's not in the set.







Bucket 4

Hash function maps objects to "buckets"

Key point: hash table lets us avoid comparing against every object in the set (provided we pick a good hash function that has few collisions)

More information:

Downey Chapter B.4

https://en.wikipedia.org/wiki/Hash_table

https://en.wikipedia.org/wiki/Hash_function

For the purposes of this course, it suffices to know that dictionaries (and the related **set** object, which we'll see soon), have faster membership checking than lists because they use hash tables.

Common pattern: dictionary as counter

Example: counting word frequencies

Naïve idea: keep one variable to keep track of each word We're gonna need a lot of variables!

Better idea: use a dictionary, keep track of only the words we see

```
1 wdcounts = dict()
2 for w in list_of_words:
3 wdcounts[w] += 1
```

This code as written won't work! It's your job in one of your homework problems to flesh this out. You may find it useful to read about the dict.get() method: https://docs.python.org/3/library/stdtypes.html#dict.get

Traversing a dictionary

Suppose I have a dictionary representing word counts...

...and now I want to display the counts for each word.

```
1 for w in wdcnt:
        print(w, wdcnt[w]
half 3
a 3
league 3
onward 1
all 1
in 1
the 2
valley 1
of 1
death 1
rode 1
six 1
```

hundred

Traversing a dictionary yields the keys, in no particular order. Typically, you'll get them in the order they were added, but this is not guaranteed, so don't rely on it.

This kind of traversal is, once again, a very common pattern when dealing with dictionaries. Dictionaries support iteration over their keys. They, like sequences, are **iterators**. We'll see more of this as the course continues.

https://docs.python.org/dev/library/stdtypes.html#iterator-types

Returning to our example, what if I want to map a (real) name to a username? E.g., I want to look up Emmy Noether's username from her real name

```
umid2name
{ 'aeinstein': 'Albert Einstein',
 'cshannon': 'Claude Shannon',
 'enoether': 'Amalie Emmy Noether',
 'kyfan': 'Ky Fan'}
                                                The keys of umid2name are the values
                                                of name2umid and vice versa. We sav
    name2umid = dict()
                                                that name2umid is the reverse lookup
    for uname in umid2name:
                                                table (or the inverse) for umid2name.
        truename = umid2name[uname]
        name2umid[truename] = uname
   name2umid
{'Albert Einstein': 'aeinstein',
 'Amalie Emmy Noether': 'enoether',
 'Claude Shannon': 'cshannon',
 'Ky Fan': 'kyfan'}
```

Returning to our example, what if I want to map a (real) name to a uniquame? E.g., I want to look up Emmy Noether's username from her real name

```
umid2name
{ 'aeinstein': 'Albert Einstein',
 'cshannon': 'Claude Shannon',
 'enoether': 'Amalie Emmy Noether',
 'kyfan': 'Ky Fan'}
    name2umid = dict()
    for uname in umid2name:
        truename = umid2name[uname]
        name2umid[truename] = uname
   name2umid
{'Albert Einstein': 'aeinstein',
 'Amalie Emmy Noether': 'enoether',
 'Claude Shannon': 'cshannon',
 'Ky Fan': 'kyfan'}
```

The keys of umid2name are the values of name2umid and vice versa. We say that name2umid is the reverse lookup table (or the inverse) for umid2name.

What if there are duplicate values? In the word count example, more than one word appears 2 times in the text... How do we deal with that?

```
1 print(wdcnt)
{'half': 3, 'a': 3, 'league': 3 onward': 1, 'all': 1, 'in': 1, 'the': 2, 'vall
1, 'six': 1, 'hundred': 1}
                                                        Here's our original word count dictionary
  1 wdcnt reverse = dict()
                                                        (cropped for readability). Some values
    for w in wdcnt:
                                                        (e.g., 1 and 3) appear more than once.
        c = wdcnt[w]
        if c in wdcnt reverse:
            wdcnt reverse[c].append(w)
       else:
                                                      Solution: map values with multiple keys
            wdcnt reverse[c] = [w]
                                                      to a list of all keys that had that value.
  8 wdcnt reverse
{1: ['onward', 'all', 'in', 'valley', 'of', 'death', 'rode', 'six', 'hundred'],
 2: ['the'],
 3: ['half', 'a', 'league']}
                                               What if there are duplicate values? In the word count
                                               example, more than one word appears 2 times in the
```

text... How do we deal with that?

```
1 print(wdcnt)
{'half': 3, 'a': 3, 'league': 3 onward': 1, 'all': 1, 'in': 1, 'the': 2, 'vall
1, 'six': 1, 'hundred': 1}
                                                        Here's our original word count dictionary
  1 wdcnt reverse = dict()
                                                        (cropped for readability). Some values
    for w in wdcnt:
                                                            1 and 3) appear more than once.
        if c in wdcnt reverse:
                                            Note: there is a more
            wdcnt reverse[c].append(w)
                                            graceful way to do this part
        else:
                                                                         es with multiple keys
                                            of the operation, mentioned
            wdcnt reverse[c] = [w]
                                                                          at had that value.
                                            in homework 2.
{1: ['onward', 'all', 'in', 'valley', 'of', 'death', 'rode', 'six', 'hundred'],
2: ['the'],
 3: ['half', 'a', 'league']}
                                               What if there are duplicate values? In the word count
                                               example, more than one word appears 2 times in the
```

text... How do we deal with that?

Keys Must be Hashable

```
1 d = dict()
  2 animals = ['cat', 'dog', 'bird', 'goat']
  3 d[animals] = 1.61803
                                           Traceback (most recent call last)
TypeError
<ipython-input-77-9fa9089d27b7> in <module>()
      1 d = dict()
      2 animals = ['cat', 'dog', 'bird', 'goat']
---> 3 d[animals] = 1.61803
TypeError: unhashable type: 'list'
```

From the documentation: "All of Python's immutable built-in objects are hashable; mutable containers (such as lists or dictionaries) are not."

https://docs.python.org/3/glossary.html#term-hashable

Dictionaries can have dictionaries as values!

Suppose I want to map pairs (x,y) to numbers.

```
times_table = dict()
for x in range(1,13):
    if x not in times_table:
        times_table[x] = dict()
for y in range(1,13):
        times_table[x][y] = x*y
times_table[7][9]
```

Each value of x maps to another dictionary.

Note: We're putting this if-statement here to illustrate that in practice, we often don't know the order in which we're going to observe the objects we want to add to the dictionary.

Dictionaries can have dictionaries as values!

Suppose I want to map pairs (x,y) to numbers.

```
times_table = dict()
for x in range(1,13):
    if x not in times_table:
        times_table[x] = dict()
for y in range(1,13):
        times_table[x][y] = x*y
times_table[7][9]
```

In a few slides we'll see a more natural way to perform this mapping in particular, but this "dictionary of dictionaries" pattern is common enough that it's worth seeing.

```
def naive fibo(n):
         if n < 0:
             raise ValueError('Negative Fibonacci number?')
         if n==0:
             return 0
                                 Raise an error. You'll need this in many of your future homeworks.
        elif n==1:
                                 https://docs.python.org/3/tutorial/errors.html#raising-exceptions
  7 8
             return 1
        else:
             return naive fibo(n-1) + naive fibo(n-2)
    for i in range(8,13):
        print(naive fibo(i))
 11
21
34
55
```

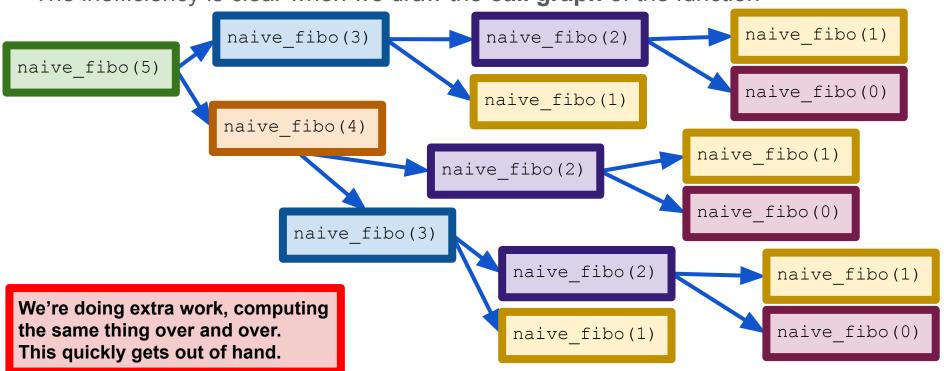
```
def naive fibo(n):
        if n < 0:
             raise ValueError('Negative Fibonacci number?')
        if n==0:
             return 0
                                 Raise an error. You'll need this in many of your future homeworks.
        elif n==1:
                                 https://docs.python.org/3/tutorial/errors.html#raising-exceptions
             return 1
  8
        else:
             return naive fibo(n-1) + naive fibo(n-2)
    for i in range(8,13):
        print(naive fibo(i))
 11
21
```

This gets slow as soon as the argument gets even moderately big. Why? 144

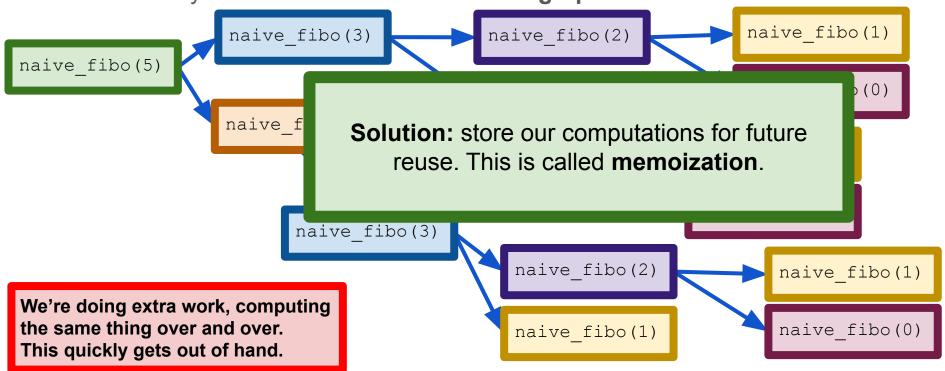
34

55

The inefficiency is clear when we draw the **call graph** of the function



The inefficiency is clear when we draw the **call graph** of the function



```
1 known = {0:0, 1:1}
2 def fibo(n):
3    if n in known:
4        return known[n]
5    else:
6        f = fibo(n-1) + fibo(n-2)
7        known[n] = f
8        return(f)
9 fibo(30)
```

This is the dictionary that we'll use for memoization. We'll store known[n] = fibo(n) the first time we compute fibo(n), and every time we need it again, we just look it up!

```
1 known = {0:0, 1:1}
2 def fibo(n):
3     if n in known:
4         return known[n]
5     else:
6         f = fibo(n-1) + fibo(n-2)
7         known[n] = f
8         return(f)
9 fibo(30)
```

If we already know the n-th Fibonacci number, there's no need to compute it again. Just look it up!

```
1 known = {0:0, 1:1}
2 def fibo(n):
3    if n in known:
4        return known[n]
5    else:
6        f = fibo(n-1) + fibo(n-2)
7        known[n] = f
8        return(f)
9 fibo(30)
```

If we don't already know it, we have to compute it, but before we return the result, we memoize it in known for future reuse.

```
1 import time
  2 start time = time.time()
    naive fibo(30)
    time.time() - start time
0.8452379703521729
  1 start time = time.time()
  2 fibo(30)
    time.time() - start time
0.00015687942504882812
```

The time difference is enormous!

Note: this was done with known set to its initial state, so this is a fair comparison.

```
1 fibo(100)

If you try to do this with naive_fibo, you'll be waiting for quite a bit!
```

```
1 fibo(100)
354224848179261915075

Our memoized Fibonacci function can compute some truly huge numbers!

1 fibo(1000)
434665576869374564356885276750406258025646605173717804024817290895
347752096896232398733224711616429964409065331879382989696499285160
```

I cropped this huge number for readability.

I cropped some of the error message for readability.

RecursionError: maximum recursion depth exceeded

Python runs out of levels of recursion. You can change this maximum recursion depth, but it can introduce instability:

https://docs.python.org/3.5/library/sys.html#sys.setrecursionlimit



bonacci function can ly huge numbers!

605173717804024817290895 I cropped this huge 331879382989696499285160

number for readability.

Traceback (most recent call last) e>()

> Python runs out of levels of recursion. You can change this maximum recursion depth, but it can introduce instability:

https://docs.python.org/3.5/library/sys.html#sy s.setrecursionlimit

```
1 known = {0:0, 1:1}
2 def fibo(n):
3    if n in known:
4        return known[n]
5    else:
6        f = fibo(n-1) + fibo(n-2)
7        known[n] = f
8        return(f)
6        Congrate dynamic
```

832040

Congratulations! You've seen your first example of dynamic programming! Lots of popular interview questions fall under this purview.

E.g., https://en.wikipedia.org/wiki/Tower_of_Hanoi

```
1 known = {0:0, 1:1}
2 def fibo(n):
3    if n in known:
4        return known[n]
5    else:
6        f = fibo(n-1) + fibo(n-2)
7        known[n] = f
8        return(f)
9 fibo(30)
```

832040

Note: the dictionary known is declared outside the function fibo. There is a good reason for this: we don't want known to disappear when we finish running fibo! We say that known is a global variable, because it is defined in the "main" program.

A name space (or namespace) is a context in which code is executed

```
The "outermost" namespace (also called a frame) is called __main__
Running from the command line or in Jupyter? You're in __main__
Often shows up in error messages, something like,

"Error ... in __main__: blah blah blah"
Variables defined in __main__ are said to be global
```

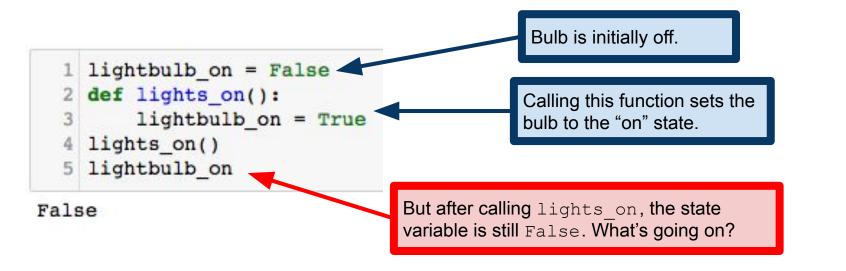
Function definitions create their own **local** namespaces

Variables defined in such a context are called **local**Local variables cannot be accessed from outside their frame/namespace

Similar behavior inside for-loops, while-loops, etc

Example: we have a program simulating a light bulb

Bulb state is represented by a global Boolean variable, lightbulb_on

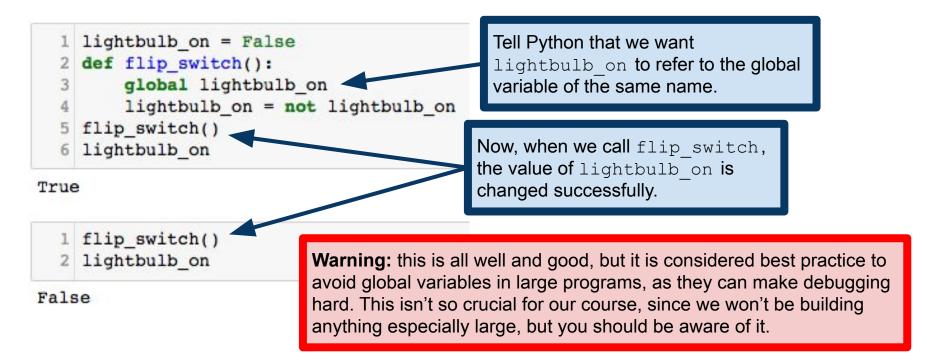


```
1 lightbulb_on = False
2 def flip_switch():
3     lightbulb_on = not lightbulb_on
4 flip_switch()
```

The fact that this code causes an error shows what is really at issue. By default, Python treats the variable <code>lightbulb_on</code> inside the function definition as being a **different** variable from the <code>lightbulb_on</code> defined in the main namespace. This is, generally, a good design. It prevents accidentally changing global state information.

```
UnboundLocalError
                                          Traceback (most recent call last)
<ipython-input-125-b39d1f83dc2a> in <module>()
      2 def flip switch():
           lightbulb on = not lightbulb on
---> 4 flip switch()
<ipython-input-125-b39d1f83dc2a> in flip switch()
      1 lightbulb on = False
     2 def flip switch():
---> 3 lightbulb on = not lightbulb on
     4 flip switch()
UnboundLocalError: local variable 'lightbulb on' referenced before assignment
```

We have to tell Python that we want lightbulb on to mean the global variable



Important note

Why is this okay, if known isn't declared global?

```
1 known = {0:0, 1:1}
2 def fibo(n):
3    if n in known:
4        return known[n]
5    else:
6        f = fibo(n-1) + fibo(n-2)
7        known[n] = f
8        return(f)
9 fibo(30)
```

Important note

Why is this okay, if known isn't declared global?

```
known = {0:0, 1:1}

def fibo(n):
    if n in known:
        return known[n]

else:
        f = fibo(n-1) + fibo(n-2)
        known[n] = f
        return(f)
known is a dictionary, and thus mutable. Maybe
mutable variables have special powers and don't
have to be declared as global?
```

Important note

Why is this okay, if known isn't declared global?

```
known = {0:0, 1:1}

def fibo(n):
    if n in known:
        return known[n]

else:
        f = fibo(n-1) + fibo(n-2)
        known[n] = f
        return(f)

fibo(30)

known is a dictionary, and thus mutable. Maybe mutable variables have special powers and don't have to be declared as global?

Correct answer: global vs local distinction is only important for variable assignment. We aren't performing any variable
```

832040

for variable assignment. We aren't performing any variable assignment in fibo, so no need for the global declaration. Contrast with lights_on, where we were reassigning lightbulb_on. Variable assignment is local by default.

Tuples

Similar to a list, in that it is a sequence of values

But unlike lists, tuples are immutable

Because they are immutable, they are hashable

So we can use tuples where we wanted to key on a list

Documentation:

https://docs.python.org/3/tutorial/datastructures.html#tuples-and-sequences https://docs.python.org/3/library/stdtypes.html#tuples

Creating Tuples

```
t = 1, 2, 3, 4, 5
  2 t
(1, 2, 3, 4, 5)
    t = (1, 2, 3, 4, 5)
    t
(1, 2, 3, 4, 5)
         'cat'
  2 t
('cat',)
      = ('cat')
```

'cat'

Tuples created with "comma notation".

Parentheses are optional, but I recommend them for ease of reading.

Python always displays tuples with parentheses.

Creating a tuple of one element requires a trailing comma. Failure to include this comma, even with parentheses, yields... not a tuple.

Creating Tuples

```
1 t1 = tuple()
 2 t1
()
  1 t2 = tuple(range(5))
  2 t2
(0, 1, 2, 3, 4)
  1 t3 = tuple('goat')
  2 t3
('g', 'o', 'a', 't')
  1 tuple([[1,2,3],[4,5,6]])
([1, 2, 3], [4, 5, 6])
  1 print(type(t2))
<class 'tuple'>
```

Can also create a tuple using the tuple() function, which will cast any sequence to a tuple whose elements are those of of the sequence.

Tuples are Sequences

```
1 t = ('a', 'b', 'c', 'd', 'e')
  2 t[0]
'a'
                                As sequences, tuples support indexing, slices, etc.
  1 t[1:4]
('b', 'c', 'd')
  1 t[-1]
'e'
                                  And of course, sequences have a length.
  1 len(t)
5
                                     Reminder: sequences support all the operations listed here:
                                     https://docs.python.org/3.3/library/stdtypes.html#typesseg
```

Tuple Comparison

Tuples support comparison, which works analogously to string ordering.

True

0-th elements are compared. If they are equal, go to the 1-th element, etc.

False

Just like strings, the "prefix" tuple is ordered first.

True

False

True

Tuple comparison is element-wise, so we only need that each element-wise comparison is allowed by Python. Tuples are Immutable

```
Tuples are immutable, so changing
  1 fruits = ('apple', 'banana', 'orange', 'kiwi')
                                                                  an entry is not permitted.
  2 fruits[2] = 'grapefruit'
TypeError
                                           Traceback (most recent call last)
<ipython-input-48-c40a1905a6e9> in <module>()
      1 fruits = ('apple', 'banana', 'orange', 'kiwi')
---> 2 fruits[2] = 'grapefruit'
TypeError: 'tuple' object does not support item assignment
                                                                  As with strings, have to make a new
                                                                  assignment to the variable.
  1 fruits = fruits[0:2] + ('grapefruit',) + fruits[3:]
  2 fruits
                                                                Note: even though 'grapefruit',
('apple', 'banana', 'grapefruit', 'kiwi')
                                                                is a tuple, Python doesn't know how to
                                                                parse this line. Use parentheses!
  1 fruits = fruits[0:2] + 'grapefruit', + fruits[3:]
```

Useful trick: tuple assignment

```
Tuples in Python allow us to make many variable assignments at
  3 print(a, b)
                              once. Useful tricks like this are sometimes called syntactic sugar.
                               https://en.wikipedia.org/wiki/Syntactic_sugar
10 5
                                   Common pattern: swap the values of two variables.
     print(a, b)
 10
     a = 10
                                      This line achieves the same end, but in a
                                      single assignment statement instead of three,
     (a,b) = (b,a)
                                      and without the extra variable tmp.
```

5 10

4 print(a, b)

Useful trick: tuple assignment

```
(x,y,z) = (2*'cat', 0.57721, [1,2,3])
                                                     Tuple assignment requires one variable on
  2 (x,y,z)
                                                     the left for each expression on the right.
('catcat', 0.57721, [1, 2, 3])
   (x,y,z) = ('a', 'b', 'c', 'd')
ValueError
                                            Traceback (most recent call last)
<ipython-input-68-e118c50f83dd> in <module>()
---> 1 (x,y,z) = ('a','b','c','d')
                                                           If the number of variables doesn't
ValueError: too many values to unpack (expected 3)
                                                           match the number of expressions,
                                                           that's an error.
   (x,y,z) = ('a','b')
ValueError
                                            Traceback (most recent call last)
<ipython-input-69-875f95cea434> in <module>()
---> 1 (x,y,z) = ('a','b')
ValueError: not enough values to unpack (expected 3, got 2)
```

Useful trick: tuple assignment

```
email = 'klevin@umich.edu'
  2 email.split('@')
['klevin', 'umich.edu']
    (user,domain) = email.split('@')
  2 user
'klevin'
    domain
'umich.edu'
 2 print(x, y, z)
```

The string.split() method returns a list of strings, obtained by splitting the calling string on the characters in its argument.

Tuple assignment works so long as the right-hand side is **any** sequence, provided the number of variables matches the number of elements on the right. Here, the right-hand side is a list, ['klevin', 'umich.edu'].

A string is a sequence, so tuple assignment is allowed. Sequence elements are characters, and indeed, x, y and z are assigned to the three characters in the string.

Tuples as Return Values

```
This function takes a list of numbers and returns a
                                                tuple summarizing the list.
    import random
                                                https://en.wikipedia.org/wiki/Five-number_summary
    def five numbers(t):
        t.sort()
        n = len(t)
        return (t[0], t[n//4], t[n//2], t[(3*n)//4], t[-1])
    five numbers ([1,2,3,4,5,6,7])
(1, 2, 4, 6, 7)
  1 randnumlist = [random.randint(1,100) for x in range(60)]
    (mini, lowg, med, upg, maxi) = five numbers(randnumlist)
  3 (mini,lowq,med,upq,maxi)
(3, 27, 54, 73, 98)
                                                           Test your understanding: what
                                                           does this list comprehension do?
```

Tuples as Return Values

More generally, sometimes you want more than one return value

```
= divmod(13,4)
  2 t
(3, 1)
     (quotient, remainder) = divmod(13,4)
  2 quotient
3
                                            divmod is a Python built-in function that takes a pair
                                            of numbers and outputs the quotient and remainder,
    remainder
                                            as a tuple. Additional examples can be found here:
                                            https://docs.python.org/3/library/functions.html
```

Useful trick: variable-length arguments

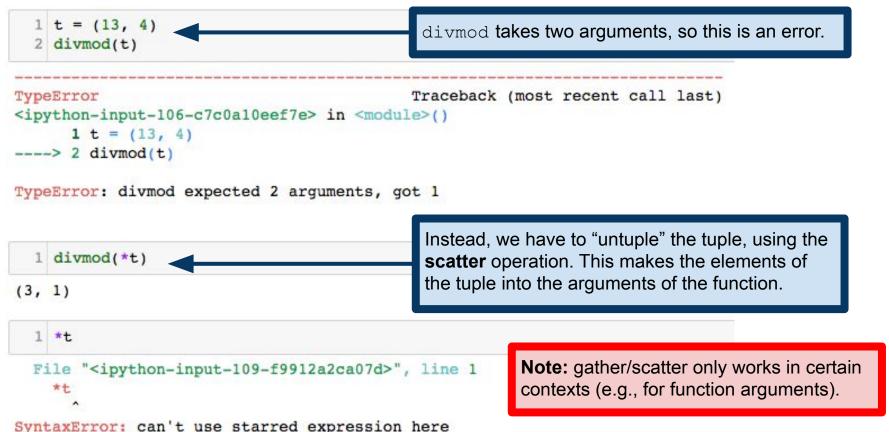
```
def my min( *args ):
        return min(args)
  3 \text{ my min}(1,2,3)
  1 my min(4,5,6,10)
  1 def print_all( *args ):
        print(args)
  3 print all('cat', 'dog', 'bird')
('cat', 'dog', 'bird')
  1 print all()
```

A parameter name prefaced with * **gathers** all arguments supplied to the function into a tuple. This is also called **argument packing**.

Note: this is also one of several ways that one can implement optional arguments, though we'll see better ways later in the course.

Gather and Scatter

The opposite of the gather operation is **scatter**



Python includes a number of useful functions for combining lists and tuples

```
1 t1 = ['apple', 'orange', 'banana', 'kiwi']
  2 t2 = [1, 2, 3, 4]
  3 zip(t1,t2)
                                        zip() returns a zip object, which is an iterator containing
                                        as its elements tuples formed from its arguments.
<zip at 0x10c95d5c8>
                                        https://docs.python.org/3/library/functions.html#zip
  1 for tup in zip(t1,t2):
         print(tup)
                                      Iterators are, in essence, objects that support for-loops. All
('apple', 1)
                                      sequences are iterators. Iterators support, crucially, a method
('orange', 2)
                                        next (), which returns the "next element". We'll see this
'banana', 3)
                                     in more detail later in the course.
('kiwi', 4)
                                      https://docs.python.org/3/library/stdtypes.html#iterator-types
```

zip () returns a zip object, which is an **iterator** containing as its elements tuples formed from its arguments.

https://docs.python.org/3/library/functions.html#zip

https://docs.python.org/3/library/stdtypes.html#typeiter

```
1 for tup in zip(['a', 'b', 'c'],[1,2,3,4]):
         print(tup)
                                                    Given arguments of different lengths,
('a', 1)
('b', 2)
                                                    zip defaults to the shortest one.
('c', 3)
  1 for tup in zip(['a', 'b', 'c', 'd'],[1,2,3]):
         print(tup)
('a', 1)
                                                   zip takes any number of arguments, so long as
('b', 2)
                                                   they are all iterable. Sequences are iterable.
('c', 3)
  1 for tup in zip([1,2,3],['a','b','c'],'xyz'):
         print(tup)
                                           Iterables are, essentially, objects that can become iterators.
(1, 'a', 'x')
(2, 'b', 'y')
                                           We'll see the distinction later in the course.
```

```
zip is especially useful for iterating
def count matches(s, t):
                                          over several lists in lockstep.
    cnt = 0
    for (a,b) in zip(s,t):
         if a==b:
             cnt += 1
    return( cnt )
count matches([1,1,2,3,5],[1,2,3,4,5])
count_matches([1,2,3,4,5],[1,2,3])
```

Test your understanding: what should this return?

```
zip is especially useful for iterating
def count matches(s, t):
                                           over several lists in lockstep.
    cnt = 0
    for (a,b) in zip(s,t):
         if a==b:
              cnt += 1
    return( cnt )
count matches([1,1,2,3,5],[1,2,3,4,5])
count_matches([1,2,3,4,5],[1,2,3])
  Test your understanding: what should this return?
```

Related function: enumerate()

```
1 for t in enumerate('goat'):
        print(t)
(3, 't')
  1 s = 'qoat'
 2 for i in range(len(s)):
        print((i,s[i]))
```

enumerate returns an **enumerate object**, which is an iterator of (index,element) pairs. It is a more graceful way of performing the pattern below, which we've seen before. https://docs.python.org/3/library/functions.html#enumerate

Dictionaries revisited

goat: 18

```
hist = {'cat':3,'dog':12,'goat':18}
hist.items()

dict_items([('cat', 3), ('dog', 12), ('goat', 18)])

for (k,v) in hist.items():
    print(k, ':', v)

cat : 3
dog : 12
dict.items() returns a dict_items object, an iterator whose elements are (key,value) tuples.
```

Dictionaries revisited

```
1 hist = {'cat':3,'dog':12,'goat':18}
  2 hist.items()
dict items([('cat', 3), ('dog', 12), ('goat', 18)])
  1 for (k,v) in hist.items():
                                         dict.items() returns a dict items object, an
        print(k, ':', v)
                                         iterator whose elements are (key,value) tuples.
cat: 3
dog : 12
goat: 18
  1 d = dict([(0,'zero'),(1,'one'),(2,'two')])
  2 d
                                           Conversely, we can create a dictionary by
{0: 'zero', 1: 'one', 2: 'two'}
                                           supplying a list of (key, value) tuples.
  1 dict( zip('cat','dog'))
{'a': 'o', 'c': 'd', 't': 'g'}
```

Tuples as Keys

```
name2umid = {('Einstein', 'Albert'): 'aeinstein',
    ('Noether', 'Emmy'): 'enoether',
    ('Shannon', 'Claude'): 'cshannon',
     ('Fan', 'Ky'): 'kyfan'}
  5 name2umid
                                               In (most) Western countries, the family name is said
                                               last (hence "last name"), but it is frequently useful to
{('Einstein', 'Albert'): 'aeinstein',
                                               key on this name before keying on a given name.
 ('Fan', 'Ky'): 'kyfan',
 ('Noether', 'Emmy'): 'enoether',
 ('Shannon', 'Claude'): 'cshannon'}
    name2umid[('Einstein', 'Albert')]
'aeinstein'
                                               Keying on tuples is especially useful for representing
  1 sparsemx = dict()
                                               sparse structures. Consider a 20-by-20 matrix in
  2 \text{ sparsemx}[(1,4)] = 1
  3 \text{ sparsemx}[(3,5)] = 1
                                               which most entries are zeros. Storing all the entries
  4 \text{ sparsemx}[(12,13)] = 2
                                               requires 400 numbers, but if we only record the
  5 \text{ sparsemx}[(11,13)] = 3
                                               entries that are nonzero...
  6 sparsemx[(19,13)] = 5
  7 sparsemx
\{(1, 4): 1, (3, 5): 1, (11, 13): 3, (12, 13): 2, (19, 13): 5\}
```

Data Structures: Lists vs Tuples

Use a **list** when:

Length is not known ahead of time and/or may change during execution Frequent updates are likely

Use a **tuple** when:

The set is unlikely to change during execution

Need to key on the set (i.e., require immutability)

Want to perform multiple assignment or use in variable-length argument list

Most code you see will use lists, because mutability is quite useful