STAT606 Computing for Data Science and Statistics

Lecture 23: TensorFlow

TensorFlow

Open source symbolic math library Popular in ML, especially for neural networks



Developed by GoogleBrain

Google's Al/Deep learning division

You may recall their major computer vision triumph circa 2012:

http://www.nytimes.com/2012/06/26/technology/in-a-big-network-of-computers-evidence-of-machine-learning.html

TensorFlow is **not** new, and **not** very special:

Many other symbolic math programs predate it!

TensorFlow is unique in how quickly it gained so much market share Open-sourced only in 2015...

...and almost immediately became the dominant framework for NNs

TensorFlow: Installation

Easiest: pip install tensorflow

Also easy: install in anaconda

More information: https://www.tensorflow.org/install/



Note: if you want to do fancier things (e.g., run on GPU instead of CPU), installation and setup gets a lot harder. For this course, we're not going to worry about it. In general, for running on a GPU, if you don't have access to a cluster with existing TF installation, you should consider paying for Amazon/GoogleCloud instances.

Aside: TensorFlow, Versions and Upgrading

In 2019, TensorFlow made a major change from version 1.X to 2.X

This new version of TensorFlow made some fundamental changes

Added built-in support for Keras https://en.wikipedia.org/wiki/Keras

Added tricks for computational speedups such as eager execution

https://en.wikipedia.org/wiki/Eager_evaluation

Streamlined code for running models (more on this soon)

These changes are all good, but the changes hide some of the most interesting stuff that TensorFlow can do! I recommend that you at least look at the old TensorFlow, which you can install with

pip install tensorflow==1.15

Note: TF v1 documentation is archived at: https://www.tensorflow.org/versions/r1.15/api_docs/python/tf

Fundamental concepts of TensorFlow

Tensor

Recall that a tensor is really just an array of numbers "Rank" of a tensor is the number of dimensions it has So, a matrix is a rank-2 tensor, vector is rank 1, scalar rank 0 A cube of numbers is a 3-tensor, and so on

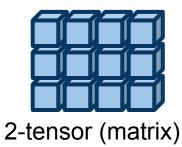
Computational graph

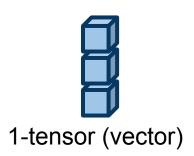
Directed graph that captures the "flow" of data through the program Nodes are operations (i.e., computations)

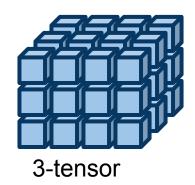
Edges represent data sent between operations

Tensors









Note: most things you read will call this dimension the *rank* of the tensor, but you should know that some mathematicians use *rank* to mean the tensor generalization of linear algebraic rank. These people will usually use the term *order* instead.

Tensors: tf. Tensor objects

Tensors are represented in TensorFlow as tf.Tensor objects

```
Every tf.Tensor object has:

data type (e.g., int, float, string, ...)

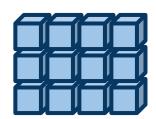
shape (e.g., 2-by-3-by-5, 5-by-5, 1-by-1, etc)

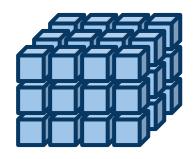
Shape encodes both rank and 'length' of each dimension
```

tf. Tensor objects are immutable with slight exceptions, which we'll talk about soon









Special tf. Tensor() objects

- tf.constant: will not change its value during your program.

 Like an immutable tensor
- tf.placeholder: gets its value from elsewhere in your program

 E.g., from training data or from results of other Tensor computations

 Note: this was removed in TensorFlow v2; now handled by tf.function (in a few slides!)
- tf.Variable: represents a tensor whose value may change during execution
 Unlike above tf.Tensor types, tf.Variables are mutable
 Useful for ML, because we want to update parameters during training
- tf.SparseTensor: most entries of a SparseTensor will be zero

 TF stores this differently; saves on memory

 Useful for applications where data is sparse, such as networks

Special tf. Tensor() objects

- tf.constant: will not change its value during your program.

 Like an immutable tensor
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 E.g., from training data or from results of other Tensor computations
 - Note: this was removed in TensorFlow v2; now handled by tf.function (in a few slides!)
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 Unlike above tf.Tensor types, tf.Variables are mutable
 Useful for ML, because we want to update parameters during training

tf man and most entries of a decomposition will be zero

For now, these three are the important ones.

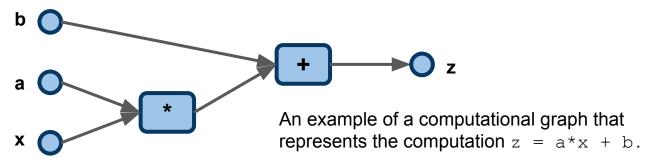
Computational Graph

From the "Getting Started" guide: "A **computational graph** is a series of TensorFlow operations arranged into a graph of nodes."

Every node takes zero or more tensors as input and outputs one or more tensors.

A TensorFlow program consists, essentially, of two sections:

- 1) Building the computational graph
- 2) Running the computational graph



TF as Dataflow

Dataflow is a term for frameworks in which computation is concerned with the **pipeline** by which the data is processed

Data transformed and combined via a series of operations

This view makes it clear when parallelization is possible...

...because dependence between operations can be read off the graph

https://en.wikipedia.org/wiki/Dataflow

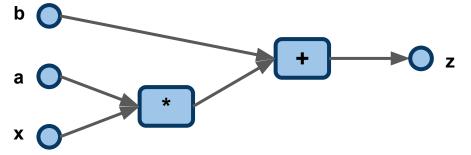
https://en.wikipedia.org/wiki/Stream_processing

This should sound familiar from PySpark!

Building the Computational Graph

```
1  a = tf.constant(2, dtype=tf.float32)
2  b = tf.constant(3, dtype=tf.float32)
3  x = tf.constant(4, dtype=tf.float32)
4  z = a*x + b
Here's a snippet of a TF program in which we define a computational graph.
```

Equivalent computational graph:

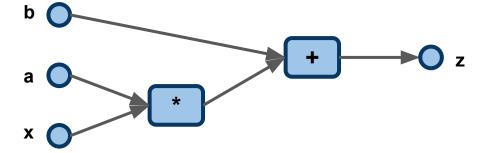


Note: strictly speaking, we haven't actually built this graph, yet. For that, we need to create a tf.Graph object, but working with this object directly is deprecated in TF version 2.

Building the Computational Graph

```
1 a = tf.constant(2, dtype=tf.float32)
2 b = tf.constant(3, dtype=tf.float32)
3 x = tf.constant(4, dtype=tf.float32)
4 z = a*x + b
```

Equivalent computational graph:



a, b and x here are constants, meaning they're fixed for the duration of our program. Really, we want to, say, let x take values from a data set and let a and b be parameters that we can tune to fit that data. We'll come back to this point.

Data types in TensorFlow

<dtype: 'string'> <dtype: 'int16'>

<dtype: 'float32'>

<dtype: 'complex64'>

```
Every {\tt tf.Tensor} () object has a data type, accessed through the {\tt dtype} attribute.
```

```
helloworld = tf.constant('hello world!')
print(helloworld.dtype)
ramanujan = tf.constant(1729, dtype=tf.int16)
print(ramanujan.dtype)
approxpi = tf.constant(3.14159, dtype=tf.float32)
print(approxpi.dtype)
imaginary = tf.constant((0.0,1.0), dtype=tf.complex64)
print(imaginary.dtype)
```

```
Note: if no dtype is specified, TF will do its best to figure it out from context, but this doesn't always go as expected, such as when you want a vector of complex numbers. When in doubt, specify!
```

Four basic data types:

Strings Integers Floats

Complex numbers

Some flexibility in specifying precision

TensorShape([3])

These are all rank-0 tensors. Yes, tf.string is a single item, and so is tf.complex.

```
helloworld = tf.constant('hello world!', dtype=tf.string)
ramanujan = tf.constant(1729, dtype=tf.int16)
approxpi = tf.constant(3.14159, dtype=tf.float32)
imaginary = tf.constant((0.0,1.0), dtype=tf.complex64)
```

To create a 1-tensor (i.e., a vector), just pass a list of scalars.

```
animals = tf.constant(['cat','dog','bird'], dtype=tf.string)
print(animals)

tf.Tensor([b'cat' b'dog' b'bird'], shape=(3,), dtype=string)
animals.shape
```

Note: all elements of a tf.Tensor must be of the same data type. The one sneaky way around this is to serialize objects to strings and store them in a tensor with dtype=tf.string.

```
onebyonemx = tf.constant([[3.1415]], dtype=tf.float32)
print(onebyonemx)
tf.Tensor([[3.1415]], shape=(1, 1), dtype=float32)
                                                              We can create a 1-by-1 matrix,
                                                              which is different from a 1-vector,
onevec = tf.constant([3.1415], dtype=tf.float32)
                                                              which is different from a scalar.
print(onevec)
tf.Tensor([3.1415], shape=(1,), dtype=float32)
scalar = tf.constant(3.1415, dtype=tf.float32)
print(scalar)
tf.Tensor(3.1415, shape=(), dtype=float32)
```

```
identity = tf.constant([[1,0,0],[0,1,0],[0,0,1]], dtype=tf.float32)
print(identity)
                                                                To create a matrix, we can
tf.Tensor(
                                                                pass a list of its rows.
[[1. 0. 0.]
 [0. 1. 0.]
 [0. 0. 1.]], shape=(3, 3), dtype=float32)
oneThruNine = tf.constant([[1,2,3],[4,5,6],[7,8,9]], dtype=tf.float32)
print(oneThruNine)
                                                      Matrix populated in row-major order.
tf.Tensor(
[[1. 2. 3.]
[4. 5. 6.]
 [7. 8. 9.]], shape=(3, 3), dtype=float32)
```

Create a 5-by-5 matrix of all ones

```
J = tf.ones([5,5])
print(J)

tf.Tensor(
[[1. 1. 1. 1. 1.]
  [1. 1. 1. 1. 1.]
  [1. 1. 1. 1. 1.]
  [1. 1. 1. 1. 1.]
  [1. 1. 1. 1.]
  [1. 1. 1. 1.], shape=(5, 5), dtype=float32)
```

```
video = tf.zeros([27,1280,720,3])
```

Create a 4-tensor, which we could use to represent one second of 720p color video (27 frames per second, 1280x720 resolution, 3 colors)

Tensor rank and shape

Rank: number of dimensions

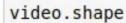
Shape: sizes of the dimensions

```
video = tf.zeros([27,1280,720,3])
print(tf.rank(video))
```

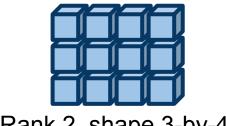
tf.Tensor(4, shape=(), dtype=int32)

```
print(video.shape)
```

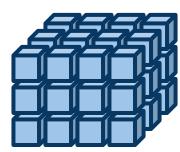
(27, 1280, 720, 3)



TensorShape([27, 1280, 720, 3])

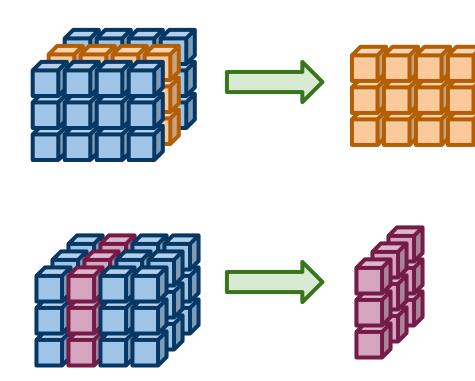


Rank 2, shape 3-by-4



Rank 3, shape 3-by-4-by-3

Note: This looks like a tuple, but it is actually its own special type, tf.TensorShape



It is often natural to refer to certain subsets of the entries of a tensor. A "subtensor" of a tensor is often called a **slice**, and the operation of picking out a slice is called **slicing** the tensor.

Tensor Indexing

```
fibovec = tf.constant([1,1,2,3,5,8,13,22], tf.int32)
print(fibovec)
tf.Tensor([ 1 1 2 3 5 8 13 22], shape=(8,), dtype=int32)
print(fibovec[0])
                                                           One index is enough to
                                                           specify a number in a
tf.Tensor(1, shape=(), dtype=int32)
                                                           vector (i.e., a 1-tensor)
J = tf.ones([3,4])
print(J)
tf.Tensor(
[[1. 1. 1. 1.]
 [1. 1. 1. 1.]
                                                          Need two indices to pick
 [1. 1. 1. 1.]], shape=(3, 4), dtype=float32)
                                                          out an entry of a matrix
                                                           (i.e., a 2-tensor)
J[1,2]
<tf.Tensor: shape=(), dtype=float32, numpy=1.0>
```

Use ':' to pick out all entries along a row or column.

```
J = tf.ones([3,4])
print(J)
tf.Tensor(
[[1. 1. 1. 1.]
 [1. 1. 1. 1.]
 [1. 1. 1. 1.]], shape=(3, 4), dtype=float32)
J[1,2]
                                                                    Create a vector from the
                                                                    second (zero-indexing!)
<tf.Tensor: shape=(), dtype=float32, numpy=1.0>
                                                                    row of the matrix.
J[1,:]
<tf.Tensor: shape=(4,), dtype=float32, numpy=array([1., 1., 1.], dtype=float32)>
J[:,2]
                                                                               Create a vector from the
                                                                               third column of the matrix.
<tf.Tensor: shape=(3,), dtype=float32, numpy=array([1., 1., 1.], dtype=float32)
```

Note: result is a "column vector" regardless of whether we slice a row or a column!

Use ':' to pick out all entries along a row or column.

```
J = tf.ones([3,4])
print(J)
tf.Tensor(
[[1. 1. 1. 1.]
 [1. 1. 1. 1.]
 [1. 1. 1. 1.]], shape=(3, 4), dtype=float32)
J[1,2]
                                                       Sidenote: the data inside a Tensor
                                                       object is really just a numpy array!
<tf.Tensor: shape=(), dtype=float32
                                    numpy=1.0>
J[1,:]
<tf.Tensor: shape=(4,), dtype=float32 numpy=array([1., 1., 1., 1.], dtype=float32)>
J[:,2]
<tf.Tensor: shape=(3,), dtype=float32 numpy=array([1., 1., 1.], dtype=float32)>
```

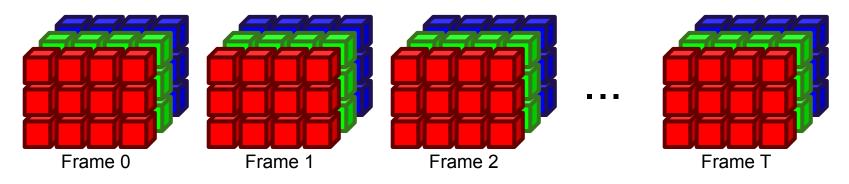
More complicated example: video processing

Four dimensions:

Pixels (height-by-width)

Three colors (RGB)

Time index (multiple frames)



More complicated example: video processing

Test your understanding:

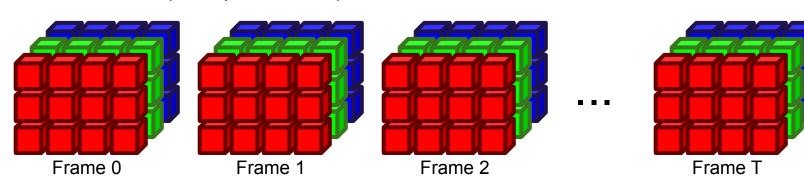
What is the rank of the "video" tensor below?

Four dimensions:

Pixels (height-by-width)

Three colors (RGB)

Time index (multiple frames)



More complicated example: video processing

Four dimensions:

Pixels (height-by-width)

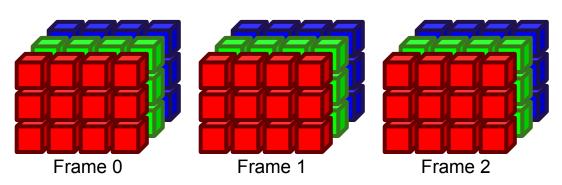
Three colors (RGB)

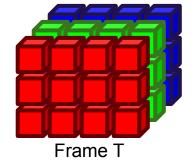
Time index (multiple frames)

Test your understanding:

What is the rank of the "video" tensor below?

Answer: 4, since there are four dimensions; height, width, color and time.





```
video = tf.zeros([27,1280,720,3])
video.shape
```

TensorShape([27, 1280, 720, 3])

```
firstframe = video[0,:,:,:] 
firstframe.shape
```

TensorShape([1280, 720, 3])

bluevideo = video[:,:,:,2] .
bluevideo.shape

TensorShape([27, 1280, 720])

redvideo = video[:,:,:,0]
redvideo.shape

TensorShape([27, 1280, 720])

Use ':' to pick out all entries along a row or column.

Pick out the 3-color 1280-by-720 image that is the first frame of the video

Pick out only the blue channel of the video (see RGB on wikipedia)

Pick out only the red channel of the video

Test your understanding:

Q: I have an x-by-y-by-z tensor. What is its rank?

Test your understanding:

Q: I have an x-by-y-by-z tensor. What is its rank?

A: 3

Q: How many elements are in this x-by-y-by-z 3-tensor?

Test your understanding:

Q: I have an x-by-y-by-z tensor. What is its rank?

A: 3

Q: How many elements are in this x-by-y-by-z 3-tensor?

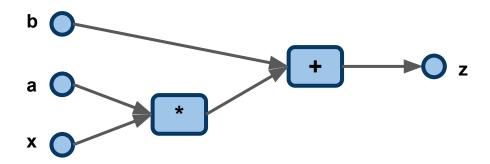
A: x*y*z

```
Reshape a 3-tensor into a
mytensor = tf.zeros([10,20,30])
                                                       4-tensor. Note that the
mytensor.shape
                                                       shapes are consistent
                                                       with one another.
TensorShape([10, 20, 30])
newtensor = tf.reshape(mytensor, [125,3,2,8])
newtensor.shape
                                                      Reshaping to an inconsistent
TensorShape([125, 3, 2, 8])
                                                      shape results in an error.
badtensor = tf.reshape(mytensor, [10,20,40])
InvalidArgumentError
                                             Traceback (most recent call last)
<ipython-input-71-fecb512dde90> in <module>
----> 1 badtensor = tf.reshape(mytensor, [10,20,40])
```

```
1 a = tf.constant(2, dtype=tf.float32)
2 b = tf.constant(3, dtype=tf.float32)
3 x = tf.constant(4, dtype=tf.float32)
4 z = a*x + b
```

In practice, we want to be able to change a and b to adjust our model. Right now, they're constants, and cannot be changed.

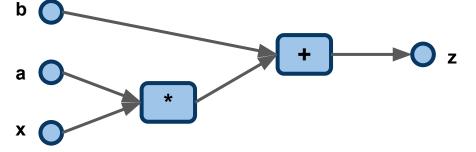
Equivalent computational graph:



```
1 a = tf.constant(2, dtype=tf.float32)
2 b = tf.constant(3, dtype=tf.float32)
3 x = tf.constant(4, dtype=tf.float32)
4 z = a*x + b
```

In practice, we want to be able to change a and b to adjust our model. Right now, they're constants, and cannot be changed.

Equivalent computational graph:



The solution is to make a and b Variable tensors.

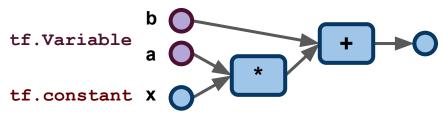
```
a = tf.Variable( 2, dtype=tf.float32)
b = tf.Variable( 3, dtype=tf.float32)
x = tf.constant( 1, dtype=tf.float32)
a*x + b

<tf.Tensor: shape=(), dtype=float32, numpy=5.0>

Change values of Variable tensors
using the assign method.

<tf.Tensor: shape=(), dtype=float32, numpy=3.0>
```

Equivalent computational graph



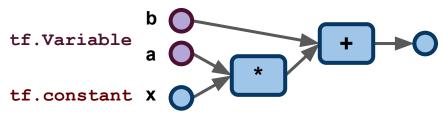
```
a = tf.Variable( 2, dtype=tf.float32)
b = tf.Variable( 3, dtype=tf.float32)
x = tf.constant( 1, dtype=tf.float32)
a*x + b

<tf.Tensor: shape=(), dtype=float32, numpy =5.0>

Change values of Variable tensors
using the assign method.

<tf.Tensor: shape=(), dtype=float32, numpy =3.0>
```

Equivalent computational graph



```
a = tf.Variable( 2, dtype=tf.float32)
b = tf.Variable( 3, dtype=tf.float32)
x = tf.constant( 1, dtype=tf.float32)
a*x + b

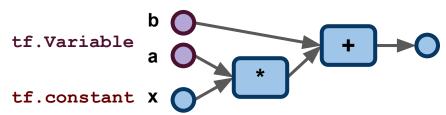
<tf.Tensor: shape=(), dtype=float32, numpy =5.0>

Change values of Variable tensors
using the assign method.

<tf.Tensor: shape=(), dtype=float32, numpy =3.0>
```

Note: in practice, we rarely need to use the assign method directly. It is mostly used under the hood by TensorFlow to change our parameters as we are fitting a model.

Equivalent computational graph



Building the computational graph: tf.function

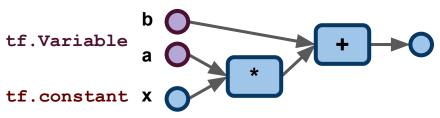
```
a = tf.Variable( 2, dtype=tf.float32)
b = tf.Variable( 3, dtype=tf.float32)
x = tf.constant( 1, dtype=tf.float32)
a*x + b

<tf.Tensor: shape=(), dtype=float32, numpy=5.0>

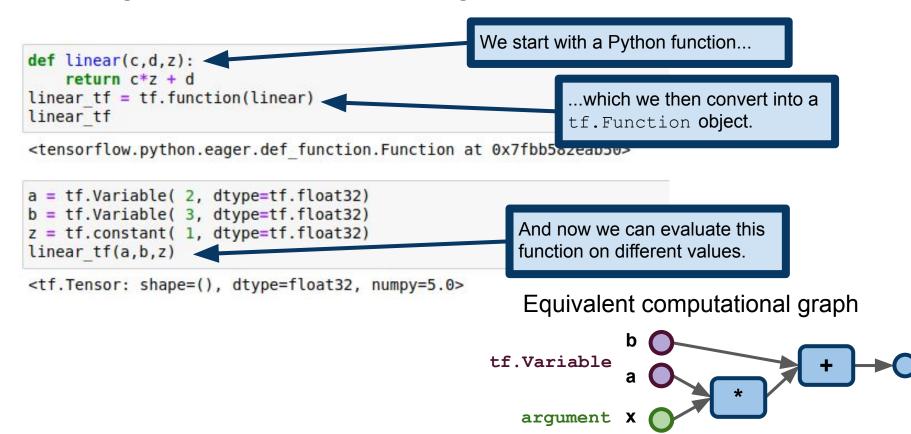
a.assign(2)
b.assign(1)
a*x + b # x is still 1; 2*1 + 1 = 3

<tf.Tensor: shape=(), dtype=float32, numpy=3.0>
```

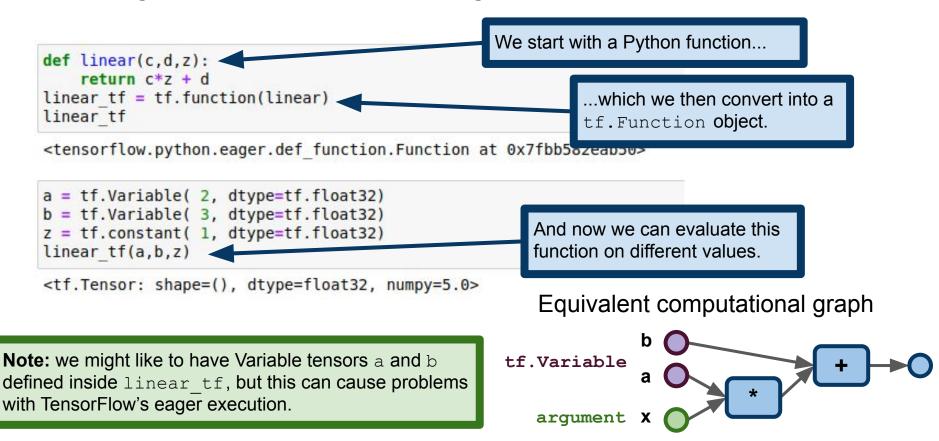
Equivalent computational graph



Building the computational graph: tf.function



Building the computational graph: tf.function



Running TensorFlow

```
Operations are defined here,
def lin comb(x,y):
                                                                    but we still haven't actually
   # Now we define some variables
                                                                    computed anything, yet...
   a = tf.constant(2, dtype=tf.float32)
   b = tf.constant(1, dtype=tf.float32)
   return a*x + b*y
linear combination = tf.function(lin comb)
linear combination
<tensorflow.python.eager.def function.Function at 0x7fbb58288460>
                                                                    Evaluate our computational
linear combination(4,2)
                                                                    graph with particular values
<tf.Tensor: shape=(), dtype=float32, numpy=10.0>
                                                                    given to x and y.
```

Running TensorFlow

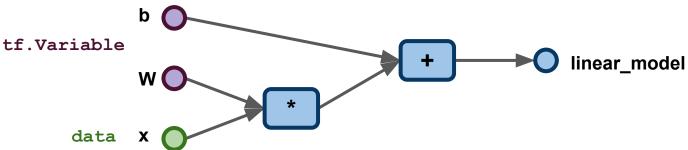
Running TensorFlow

```
Operations are defined here,
def lin comb(x,y):
                                                                    but we still haven't actually
   # Now we define some variables
                                                                    computed anything, yet...
   a = tf.constant(2, dtype=tf.float32)
   b = tf.constant(1, dtype=tf.float32)
   return a*x + b*y
linear combination = tf.function(lin comb)
linear combination
<tensorflow.python.eager.def function.Function at 0x7fbb58288460>
                                                           Once our tf. Function is defined, we
linear combination(4,2)
                                                           can evaluate it on a collection of
<tf.Tensor: shape=(), dtype=float32, numpy=10.0>
                                                           arguments. For example, we might want to
                                                           pass in a collection of (x,y) pairs.
linear combination([4,3,2,1], [2,3,4,5]
<tf.Tensor: shape=(4,), dtype=float32, numpy=array([10., 9., 8., 7.], dtype=float32)>
```

```
def linear_prediction_pyfn(c,d,x):
    return c*x + d
linear_model = tf.function(linear_prediction_pyfn)

W = tf.Variable([0.5], dtype=tf.float32)
b = tf.Variable([-1], dtype=tf.float32)
linear_model(W,b,[0,1,2,3,4])

<tf.Tensor: shape=(5,), dtype=float32, numpy=array([-1. , -0.5, 0. , 0.5, 1. ], dtype=float32)>
```



data

```
We're using c and d in the function
                                                        Model: y = Wx + b
                                                                                 arguments just to avoid confusion
def linear prediction pyfn(c,d,x):
                                                                                 with the global variables w and b.
    return c*x + d
linear model = tf.function(linear prediction pyfn)
                                                             w and b are both rank-1 tensors, with
W = tf.Variable([0.5], dtype=tf.float32)
b = tf.Variable([-1], dtype=tf.float32)
                                                             values 0.5 and -1, respectively.
linear model(W, b, [0, 1, 2, 3, 4])
<tf.Tensor: shape=(5,), dtype=float32, numpy=array([-1. , -0.5, 0. , 0.5, 1. ], dtype=float32)>
                tf.Variable
                                                                                      linear model
```

```
def linear prediction pyfn(c,d,x):
    return c*x + d
linear model = tf.function(linear prediction pyfn)
W = tf.Variable([0.5], dtype=tf.float32)
                                               Atf. Variable can be a Tensor of any type and shape.
b = tf.Variable([-1], dtype=tf.float32)
                                               The type and shape of the variable are specified by the
tilleal modet(W,D,[0,1,2,3,4])
                                               initialization. After construction, the value can be changed
<tf.Tensor: shape=(5,), dtype=float32, numpy
                                               using the assign method that we saw earlier.
                tf.Variable
                                                                                  linear model
                       data
```

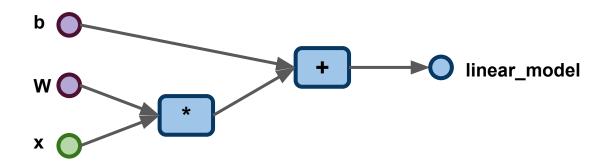
data

```
def linear prediction pyfn(c,d,x):
    return c*x + d
linear model = tf.function(linear prediction pyfn)
W = tf.Variable([0.5], dtype=tf.float32)
                                                          Evaluate the model with
b = tf.Variable([-1], dtype=tf.float32)
                                                          different values of x.
linear model(W,b,[0,1,2,3,4]) \blacktriangleleft
<tf.Tensor: shape=(5,), dtype=float32, numpy=array([-1. , -0.5, 0. , 0.5, 1. ], dtype=float32)>
                tf.Variable
                                                                                   linear model
```

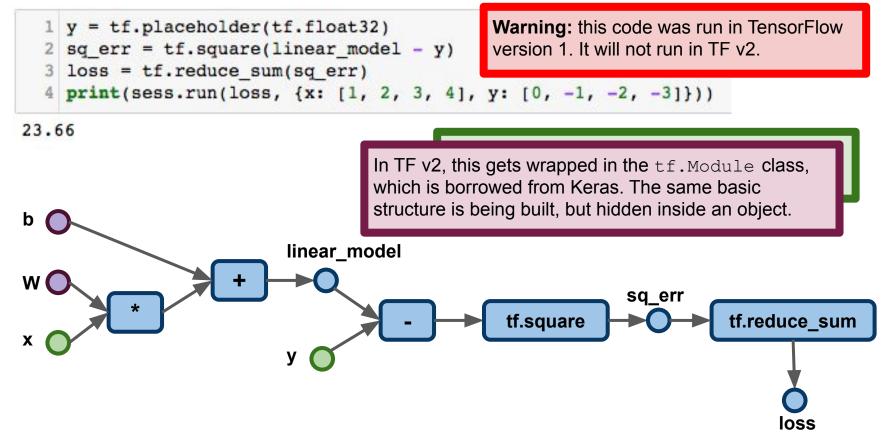
So far, we have a circuit that computes a linear regression estimate

To train our model, we need:

- 1) A loss function
- 2) An argument y for the training data dependent values

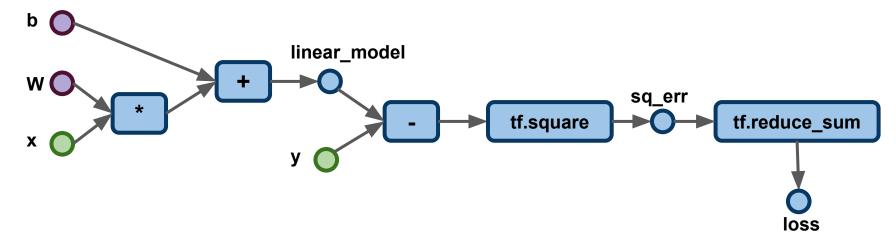


```
1 y = tf.placeholder(tf.float32)
                                                  Warning: this code was run in TensorFlow
  2 sq err = tf.square(linear model - y)
                                                  version 1. It will not run in TF v2.
    loss = tf.reduce sum(sq err)
   print(sess.run(loss, {x: [1, 2, 3, 4], y: [0, -1, -2, -3]}))
23.66
                                             In TF v1, we could just keep building out this
                                             graph to define a loss function.
                            linear_model
                                                                sq_err
                                                   tf.square
                                                                           tf.reduce_sum
```

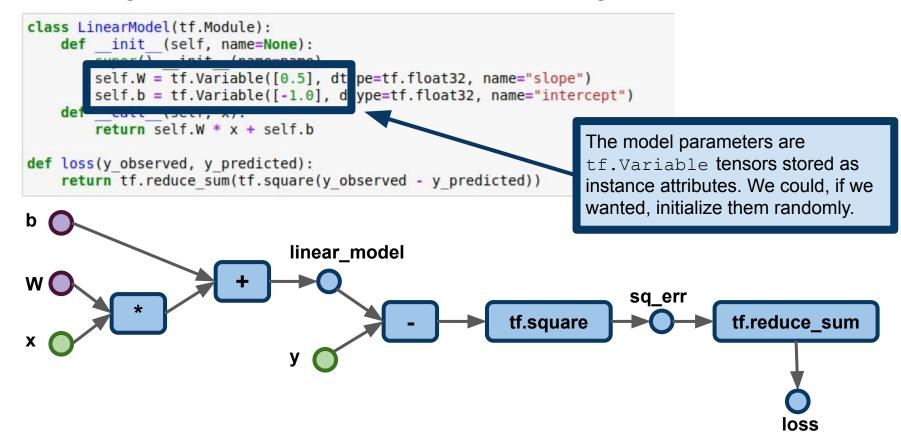


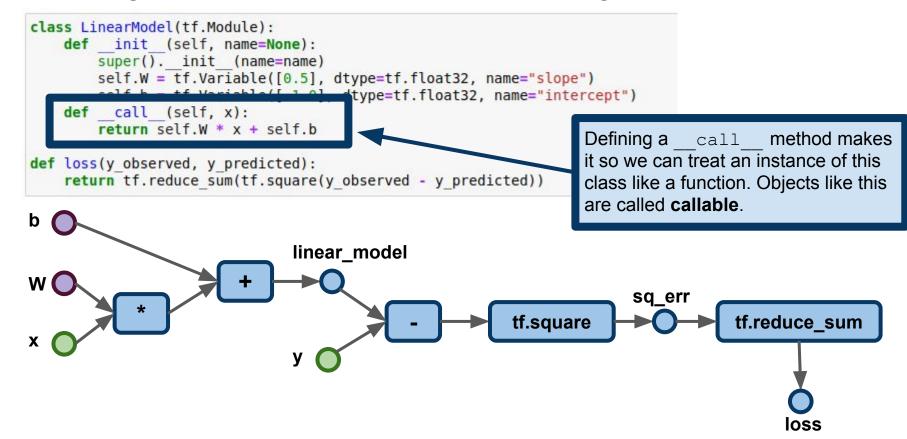
```
class LinearModel(tf.Module):
    def __init__(self, name=None):
        super().__init__(name=name)
        self.W = tf.Variable([0.5], dtype=tf.float32, name="slope")
        self.b = tf.Variable([-1.0], dtype=tf.float32, name="intercept")
    def __call__(self, x):
        return self.W * x + self.b

def loss(y_observed, y_predicted):
    return tf.reduce_sum(tf.square(y_observed - y_predicted))
```



```
class LinearModel(tf.Module):
                 init
                       (name=name)
                                     pe=tf.float32, name="slope")
        self.b = tf.Variable([-1.0], dtype-tf.float32, name="intercept")
   def call (self, x):
        return self.W * x + self.b
                                                                  The Python super () function
                                                                  accesses the parent class (i.e., the
def loss(y observed, y predicted):
    return tf.reduce sum(tf.square(y observed - y predicted))
                                                                  class we are inheriting from).
                               linear_model
                                                                       sq_err
                                                        tf.square
                                                                                   tf.reduce sum
                                                                                         loss
```

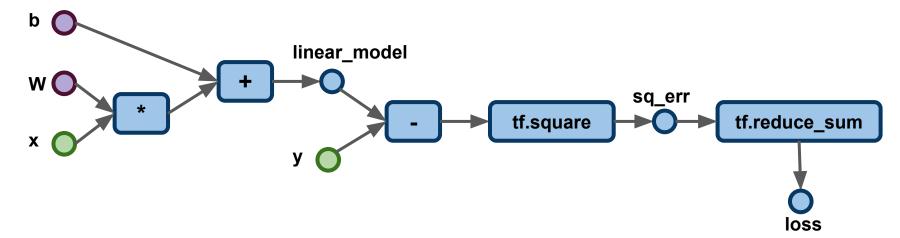




```
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def __call__(self, x):
    return self.W * x + self.b

def loss(y_observed, y_predicted):
    return tf.reduce_sum(tf.square(y_observed - y_predicted))
Note: tf.reduce_sum does
just what you think it does!
```



return tf.reduce sum(tf.square(y observed - y predicted))

Note: As you can see, the computational graph can get very complicated very quickly. TensorFlow has a set of built-in tools, collectively called **TensorBoard**, for handling some of this complexity:

https://www.tensorflow.org/tensorboard/graphs

```
class LinearModel(tf.Module):
   def init (self, name=None):
       super(). init (name=name)
       self.W = tf.Variable([0.5], dtype=tf.float32, name="slope")
        self.b = tf.Variable([-1.0], dtype=tf.float32, name="intercept")
   def call (self, x):
        return self.W * x + self.b
def loss(y observed, y predicted):
    return tf.reduce sum(tf.square(y observed - y predicted))
x = tf.constant([1,2,3,4], dtype=tf.float32)
                                                                Give (x,y) values to the model,
y = tf.constant([0,-1,-2,-3], dtype=tf.float32)
                                                                evaluate its ability to replicate
loss( linear model(x), y ).numpy()
                                                                the observed y values.
23.5
                           linear model
                                                                      sq err
                                                       tf.square
                                                                                  tf.reduce sum
```

loss

```
class LinearModel(tf.Module):
   def init (self, name=None):
       super(). init (name=name)
       self.W = tf.Variable([0.5], dtype=tf.float32, name="slope")
       self.b = tf.Variable([-1.0], dtype=tf.float32, name="intercept")
   def call (self, x):
       return self.W * x + self.b
def loss(y observed, y predicted):
   return tf.reduce sum(tf.square(y observed - y predicted))
x = tf.constant([1,2,3,4], dtype=tf.float32)
                                                      The numpy () method retrieves
y = tf.constant([0,-1,-2]
                                   =tf.float32 )
                                                      the actual numpy object from
loss( linear model(x), y .numpy(
                                                      inside the tf. Tensor.
23.5
                           linear model
                                                                     sq err
                                                       tf.square
                                                                                 tf.reduce_sum
                                                                                       loss
```

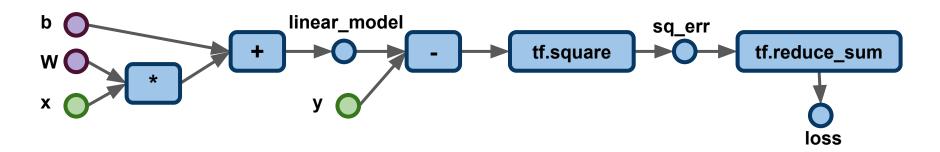
```
x = tf.constant( [1,2,3,4], dtype=tf.float32 )
y = tf.constant( [0,-1,-2,-3], dtype=tf.float32 )
loss( linear_model(x), y ).numpy()

23.5

How can we improve (i.e., decrease) this loss?
```

Option 1: set w and b manually.

We know W=-1, b=1 is the correct answer
Change values of tf. Variables using assign method



```
x = tf.constant( [1,2,3,4], dtype=tf.float32 )
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23.5

How can we improve (i.e., decrease) this loss?
```

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We know W=-1, b=1 is the correct answer

Change values of tf. Variables using assign method

```
linear_model.W.assign([-1])
linear_model.b.assign([1])
loss( linear_model(x), y ).numpy()
Update the slope and intercept in the model to the correct values.
```

0.0

```
x = tf.constant( [1,2,3,4], dtype=tf.float32 )
y = tf.constant( [0,-1,-2,-3], dtype=tf.float32 )
loss( linear_model(x), y ).numpy()

23.5

How can we improve (i.e., decrease) this loss?
```

Option 1: set w and b manually.

We know W=-1, b=1 is the correct answer

Change values of tf. Variables using assign method

Note: because W and b are rank-1 tensors, we have to pass their new values as length-1 lists, not scalars.

linear_model.W.assign(-1) would result in an error.

```
x = tf.constant( [1,2,3,4], dtype=tf.float32 )
y = tf.constant( [0,-1,-2,-3], dtype=tf.float32 )
loss( linear_model(x), y ).numpy()

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Option 2: use closed-form solution for loss-minimizing w and b.

...but then what happens when we have a model with no closed-form solution?

```
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y = tf.constant( [0,-1,-2,-3], dtype=tf.float32 )
loss( linear_model(x), y ).numpy()

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Option 3: take advantage of automatic differentiation

Allows easy implementation of gradient descent and related techniques

```
x = tf.constant([1,2,3,4], dtype=tf.float32)
 y = tf.constant([0,-1,-2,-3], dtype=tf.float32)
 loss( linear model(x), y ).numpy()
 23.5
                       How can we improve (i.e., decrease) this loss?
Option 1: set w and b manually.
     We know W=-1, b=1 is the correct answer
```

Change values of tf. Variables using assign method

Option 2: use close This is why we use TensorFlow! ...but then wha

Wandb. with no closed-form solution?

Option 3: take advantage of automatic differentiation

Allows easy implementation of gradient descent and related techniques

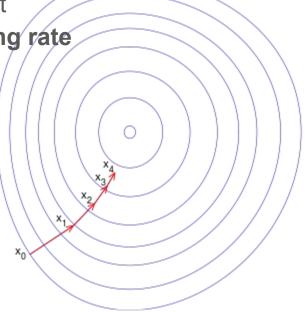
Gradient Descent: Crash Course

Iterative optimization method for minimizing a function

At location (w, b), take gradient of loss function with respect to parameters

Take a **gradient step** in the direction of the gradient

Size of step changes over time according to learning rate



Gradient Descent: Crash Course

Iterative optimization method for minimizing a function

At location (w, b), take gradient of loss function with respect to parameters

Take a **gradient step** in the direction of the gradient

Size of step changes over time according to learning rate

In short, gradient descent is a method for minimizing a function, provided we can compute its gradient (i.e., derivative). It's enough for this course to treat this as a black box.

For more information:

- S. P. Boyd and L. Vandenberghe (2004). Convex Optimization. Cambridge University Press.
- J. Nocedal and S. J. Wright (2006). *Numerical Optimization*. Springer.

```
def train(model, x, y, learning_rate):
    with tf.GradientTape() as t:
        current_loss = loss(y, model(x))

    (dW, db) = t.gradient(current_loss, [model.W, model.b])

    model.W.assign_sub( learning_rate*dW )
    model.b.assign_sub( learning_rate*db )
```

Define a train function, which takes a single gradient step with respect to a model's performance with respect to a loss function on data x and y, with a given learning rate.

```
def train(model, x, y, learning_rate):
    with tf.GradientTape() as t:
        current_loss = loss(y, model(x))

    (dW, db) = t.gradient(current_loss, [model.W, model.b])

    model.W.assign_sub( learning_rate*dW )
    model.b.assign_sub( learning_rate*db )
```

The tf.GradientTape object keeps track of our gradients. This is especially useful when we want to check whether or not our estimates have converged. Here, we just need it to do automatic differentiation for us.

```
def train(model, x, y, learning_rate):
    with tf.GradientTape() as t:
        current_loss = loss(y, model(x))

    (dW, db) = t.gradient(current_loss, [model.W, model.b])

    model.W.assign_sub( learning_rate*dW )
    model.b.assign_sub( learning_rate*db )

Use the tf.GradientTape() as t:
    current_loss = loss(y, model.W, model.b])
```

Use the tf.GradientTape to compute the gradient of the loss with respect to the current model parameters.

Caution: notice that loss is a Python function, and current_loss is a tf.Tensor that is output by that function. Breaking this pattern is a common source of bugs.

```
def train(model, x, y, learning_rate):
    with tf.GradientTape() as t:
        current_loss = loss(y, model(x))

    (dW, db) = t.gradient(current_loss, [model.W, model.b])

    model.W.assign_sub( learning_rate*dW )
    model.b.assign_sub( learning_rate*db )
```

Update the parameters. assign_sub is the tf. Variable analogue of writing x = x-dx.

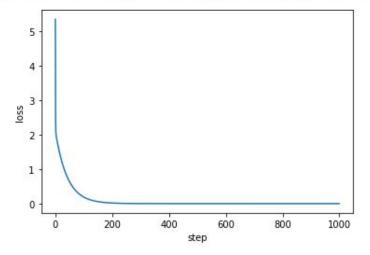
```
with tf.GradientTape() as t:
        current loss = loss(y, model(x))
    (dW, db) = t.gradient(current loss, [model.W, model.b])
   model.W.assign sub( learning rate*dW )
   model.b.assign sub( learning rate*db )
x = tf.constant([1,2,3,4], dtype=tf.float32)
                                                     Initialize the model parameters randomly.
y = tf.constant([0,-1,-2,-3], dtype=tf.float32)
                                                     tf.random.normal is similar to numpy/scipy
                                                     RNGs. Note that we need our random variables to
linear model.W.assign(tf.random.normal(shape=[1]))
                                                     be shape=[1] to match the shapes of W and b.
linear model.b.assign(tf.random.normal(shape=[1]))
(linear model.W.numpy(), linear model.b.numpy())
(array([-0.49148715], dtype=float32), array([0.48135814], dtype=float32))
```

def train(model, x, y, learning rate):

```
def train(model, x, y, learning rate):
    with tf.GradientTape() as t:
        current loss = loss(y, model(x))
    (dW, db) = t.gradient(current loss, [model.W, model.b])
    model.W.assign sub( learning rate*dW )
    model.b.assign sub( learning rate*db )
x = tf.constant([1,2,3,4], dtype=tf.float32)
y = tf.constant([0,-1,-2,-3], dtype=tf.float32)
linear model.W.assign(tf.random.normal(shape=[1]))
linear model.b.assign(tf.random.normal(shape=[1]))
(linear model.W.numpy(), linear model.b.numpy())
(array([-0.49148715], dtype=float32), array([0.48135814], dtype=float32)
                                                                    Each iteration of this loop
                                                                    computes one gradient step and
for i in range(1000):
                                                                    updates the variables accordingly.
    train(linear model, x, y, learning rate=0.01)
(linear model.W.numpy(), linear model.b.numpy())
(array([-0.9999991], dtype=float32), array([0.99999744], dtype=float32))
```

```
x = tf.constant( [1,2,3,4], dtype=tf.float32 )
y = tf.constant( [0,-1,-2,-3], dtype=tf.float32 )
linear_model.W.assign([0.5])
linear_model.b.assign([-0.5])
(linear_model.W.numpy(), linear_model.b.numpy())

losses = list(range(1000))
for i in range(1000):
    train(linear_model, x, y, learning_rate=0.01)
    losses[i] = loss(linear_model(x), y)
plt.xlabel('step'); plt.ylabel('loss'); _ = plt.plot(losses);
```



Note: TensorBoard includes a set of tools for visualization, including for tracking loss, but the approach here is quicker and easier for our purposes.

TensorFlow Estimators API: tf.estimators

tf.estimators is a TF module that simplifies model training and evaluation

Module allows one to run models on CPU or GPU, local or on GCP, etc

Simplifies much of the work of building the graph and estimating parameters

More information:

https://www.tensorflow.org/guide/estimator

Note: Keras in TensorFlow v2 serves similar purpose for specifying neural nets https://www.tensorflow.org/guide/keras