STAT606 Computing for Data Science and Statistics

Lecture 23: TensorFlow

TensorFlow

Open source symbolic math library Popular in ML, especially for neural networks

Developed by GoogleBrain

Google's AI/Deep learning division

You may recall their major computer vision triumph circa 2012:

http://www.nytimes.com/2012/06/26/technology/in-a-big-network-of-computers-evidence-of-machine-learning.html

TensorFlow is **not** new, and **not** very special:

Many other symbolic math programs predate it!

TensorFlow is unique in how quickly it gained so much market share Open-sourced in 2015...

...and almost immediately became the dominant framework for NNs



TensorFlow: Installation

Easiest: pip install tensorflow

Also easy: install in anaconda

More information: <u>https://www.tensorflow.org/install/</u>



Note: if you want to do fancier things (e.g., run on GPU instead of CPU), installation and setup gets a lot harder. For this course, we're not going to worry about it. In general, for running on a GPU, if you don't have access to a cluster with existing TF installation, you should consider paying for Amazon/GoogleCloud instances.

Aside: TensorFlow, Versions and Upgrading

In 2019, TensorFlow made a major change from version 1.X to 2.X

This new version of TensorFlow made some fundamental changes Added built-in support for Keras <u>https://en.wikipedia.org/wiki/Keras</u> Added tricks for computational speedups such as eager execution <u>https://en.wikipedia.org/wiki/Eager_evaluation</u> Streamlined code for running models (more on this soon)

These changes are all good, but the changes hide some of the most interesting stuff that TensorFlow can do! I recommend that you at least look at the old TensorFlow, which you can install with pip install tensorflow==1.15 Note: TF v1 documentation is archived at: <u>https://www.tensorflow.org/versions/r1.15/api_docs/python/tf</u>

Fundamental concepts of TensorFlow

Tensor

Recall that a tensor is really just an array of numbers "Rank" of a tensor is the number of dimensions it has So, a matrix is a rank-2 tensor, vector is rank 1, scalar rank 0 A cube of numbers is a 3-tensor, and so on

Computational graph

Directed graph that captures the "flow" of data through the program Nodes are operations (i.e., computations) Edges represent data sent between operations



Note: most things you read will call this dimension the *rank* of the tensor, but you should know that some mathematicians use *rank* to mean the tensor generalization of linear algebraic rank. These people will usually use the term *order* instead.

Tensors: tf.Tensor objects

Tensors are represented in TensorFlow as tf.Tensor objects

Every tf.Tensor object has: data type (e.g., int, float, string, ...) shape (e.g., 2-by-3-by-5, 5-by-5, 1-by-1, etc) Shape encodes both rank and 'length' of each dimension

tf.Tensor objects are immutable

with slight exceptions, which we'll talk about soon









Special tf.Tensor() objects

tf.constant: will not change its value during your program. Like an immutable tensor

tf.placeholder: gets its value from elsewhere in your program
E.g., from training data or from results of other Tensor computations
Note: this was removed in TensorFlow v2; now handled by tf.function (in a few slides!)

tf.Variable: represents a tensor whose value may change during execution Unlike above tf.Tensor types, tf.Variables are mutable Useful for ML, because we want to update parameters during training

tf.SparseTensor: most entries of a SparseTensor will be zero

TF stores this differently; saves on memory Useful for applications where data is sparse, such as networks

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tf

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For now, these three are the important ones.

Computational Graph

From the "Getting Started" guide: "A **computational graph** is a series of TensorFlow operations arranged into a graph of nodes."

Every node takes zero or more tensors as input and outputs one or more tensors.

A TensorFlow program consists, essentially, of two sections:

- 1) Building the computational graph
- 2) Running the computational graph



TF as Dataflow

Dataflow is a term for frameworks in which computation is concerned with the **pipeline** by which the data is processed

- Data transformed and combined via a series of operations
- This view makes it clear when parallelization is possible...
- ...because dependence between operations can be read off the graph

https://en.wikipedia.org/wiki/Dataflow

https://en.wikipedia.org/wiki/Stream_processing

This should sound familiar from PySpark!

Building the Computational Graph



Equivalent computational graph:



Note: strictly speaking, we haven't actually built this graph, yet. For that, we need to create a tf.Graph object, but working with this object directly is deprecated in TF version 2.

Building the Computational Graph







a, b and x here are constants, meaning they're fixed for the duration of our program. Really, we want to, say, let x take values from a data set and let a and b be parameters that we can tune to fit that data. We'll come back to this point.

Data types in TensorFlow

Every tf.Tensor() object has a data type, accessed through the dtype attribute.

```
1 helloworld = tf.constant('hello world!')
```

```
2 print(helloworld.dtype)
3 ramanujan = tf.constant(1729, dtype=tf.int16)
```

approxpi = tf.constant(3.14159, dtype=tf.float32)

imaginary = tf.constant((0.0,1.0), dtype=tf.complex64)

Four basic data types: Strings Integers Floats Complex numbers

Some flexibility in specifying precision

<dtype: 'string'> <dtype: 'int16'> <dtype: 'float32'> <dtype: 'complex64'>

4

5

print(ramanujan.dtype)

print(approxpi.dtype)

print(imaginary.dtype)

Note: if no dtype is specified, TF will do its best to figure it out from context, but this doesn't always go as expected, such as when you want a vector of complex numbers. When in doubt, specify!



Creating Tensors



tf.Tensor(3.1415, shape=(), dtype=float32)

Creating Tensors

```
identity = tf.constant([[1,0,0],[0,1,0],[0,0,1]], dtype=tf.float32)
print(identity)
```

tf.Tensor([[1. 0. 0.] [0. 1. 0.] [0. 0. 1.]], shape=(3, 3), dtype=float32) To create a matrix, we can pass a list of its rows.

```
oneThruNine = tf.constant([[1,2,3],[4,5,6],[7,8,9]], dtype=tf.float32)
print(oneThruNine)
```





Tensor rank and shape

Rank: number of dimensions

Shape: sizes of the dimensions

video = tf.zeros([27,1280,720,3]) print(tf.rank(video))

tf.Tensor(4, shape=(), dtype=int32)

print(video.shape) (27, 1280, 720, 3) video.shape **Note:** This looks like a tuple, but it is actually its TensorShape([27, 1280, 720, 3]) own special type, tf. TensorShape



Rank 2, shape 3-by-4



Rank 3, shape 3-by-4-by-3





It is often natural to refer to certain subsets of the entries of a tensor. A "subtensor" of a tensor is often called a **slice**, and the operation of picking out a slice is called **slicing** the tensor.

Tensor Indexing



<tf.Tensor: shape=(), dtype=float32, numpy=1.0>



Note: result is a "column vector" regardless of whether we slice a row or a column!

Use ':' to pick out all entries along a row or column.

J = tf.ones([3,4])
print(J)

tf.Tensor(

- [[1. 1. 1. 1.]
- [1. 1. 1. 1.]
 [1. 1. 1. 1.]], shape=(3, 4), dtype=float32)

J[1,2]	Sidenote: the data inside a Tensor
<tf.tensor: dtype="float32" numpy="1.0" shape="(),"></tf.tensor:>	object is really just a numpy array!
J[1,:]	
<tf.tensor: dtype="float32," numpy="array([</td" shape="(4,),"><td>1., 1., 1., 1.], dtype=float32)></td></tf.tensor:>	1., 1., 1., 1.], dtype=float32)>
J[:,2]	
<tf.tensor: dtype="float32," numpy="array([</td" shape="(3,),"><td>1., 1., 1.], dtype=float32)></td></tf.tensor:>	1., 1., 1.], dtype=float32)>

More complicated example: video processing

Four dimensions:

- Pixels (height-by-width)
- Three colors (**RGB**)

Time index (multiple frames)



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Test your understanding: What is the rank of the "video" tensor below?

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Four dimensions:

- Pixels (height-by-width)
- Three colors (**RGB**)
- Time index (multiple frames)

Test your understanding: What is the rank of the "video" tensor below?

Answer: 4, since there are four dimensions; height, width, color and time.



Tensor Slices Use ':' to pick out all entries along a row or column. video = tf.zeros([27,1280,720,3]) video.shape TensorShape([27, 1280, 720, 3]) Pick out the 3-color 1280-by-720 image that is firstframe = video[0,:,:,:] the first frame of the video firstframe.shape TensorShape([1280, 720, 3]) Pick out only the blue bluevideo = video[:,:,:,2] channel of the video (see bluevideo.shape RGB on wikipedia) TensorShape([27, 1280, 720]) redvideo = video[:,:,:,0] -Pick out only the red redvideo.shape channel of the video TensorShape([27, 1280, 720])

Test your understanding:

Q: I have an x-by-y-by-z tensor. What is its rank?

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A: 3

Q: How many elements are in this x-by-y-by-z 3-tensor?

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A: 3

Q: How many elements are in this x-by-y-by-z 3-tensor?

A: x*y*z





In practice, we want to be able to change a and b to adjust our model. Right now, they're constants, and cannot be changed.

Equivalent computational graph:





In practice, we want to be able to change a and b to adjust our model. Right now, they're constants, and cannot be changed.

Equivalent computational graph:



The solution is to make a and b Variable tensors.











Note: in practice, we rarely need to use the assign method directly. It is mostly used under the hood by TensorFlow to change our parameters as we are fitting a model.


Building the computational graph: tf.function

```
a = tf.Variable( 2, dtype=tf.float32)
b = tf.Variable( 3, dtype=tf.float32)
x = tf.constant( 1, dtype=tf.float32)
a*x + b
```

The predictor \times is still a constant. What if I want to plug in new data to this linear model?

<tf.Tensor: shape=(), dtype=float32, numpy=5.0>

```
a.assign(2)
b.assign(1)
a*x + b # x is still 1; 2*1 + 1 = 3
```

<tf.Tensor: shape=(), dtype=float32, numpy=3.0>



Building the computational graph: tf.function



Building the computational graph: tf.function



Running TensorFlow

<pre>def lin_comb(x,y): # Now we define some variables a = tf.constant(2, dtype=tf.float32) b = tf.constant(1, dtype=tf.float32) return a*x + b*y linear_combination = tf.function(lin_comb) linear_combination</pre>		Operations are defined here, but we still haven't actually computed anything, yet	
<tensorflow.python.eager.def_function.function 0x7fbb58288460="" at=""></tensorflow.python.eager.def_function.function>			
<pre>linear_combination(4,2) <tf.tensor: dtype="float32," numpy="10.0" shape="(),"></tf.tensor:></pre>		Evaluate our computational graph with particular values given to x and y .	

Running TensorFlow



Note that we have the constants a and b defined locally in the function, this time. This is only an issue for Variable tensors.

```
linear_combination
<tensorflow.python.eager.def function.Function at 0x7fbb58288460>
```

```
linear combination(4,2)
```

<tf.Tensor: shape=(), dtype=float32, numpy=10.0>

Running TensorFlow

<pre>def lin_comb(x,y): # Now we define some variables a = tf.constant(2, dtype=tf.float32) b = tf.constant(1, dtype=tf.float32) return a*x + b*y</pre>	but we still haven't actually computed anything, yet	
<pre>linear_combination = tf.function(lin_comb) linear_combination</pre>		
<tensorflow.python.eager.def_function.function 0x7fbb582<="" at="" td=""><td>288460></td></tensorflow.python.eager.def_function.function>	288460>	
linear_combination(4,2)	Once our tf.Function is defined, we can evaluate it on a collection of arguments. For example, we might want to pass in a collection of (x,y) pairs.	
<tf.tensor: dtype="float32," numpy="10.0" shape="(),"></tf.tensor:>		
linear_combination([4,3,2,1], [2,3,4,5])		

<tf.Tensor: shape=(4,), dtype=float32, numpy=array([10., 9., 8., 7.], dtype=float32)>

```
def linear_prediction_pyfn(c,d,x):
    return c*x + d
linear_model = tf.function(linear_prediction_pyfn)
W = tf.Variable([0.5], dtype=tf.float32)
b = tf.Variable([-1], dtype=tf.float32)
linear_model(W,b,[0,1,2,3,4])
```

<tf.Tensor: shape=(5,), dtype=float32, numpy=array([-1. , -0.5, 0. , 0.5, 1.], dtype=float32)>





<tf.Tensor: shape=(5,), dtype=float32, numpy=array([-1. , -0.5, 0. , 0.5, 1.], dtype=float32)>



data







So far, we have a circuit that computes a linear regression estimate

To train our model, we need:

- 1) A loss function
- 2) An argument y for the training data dependent values

















Note: As you can see, the computational graph can get very complicated very quickly. TensorFlow has a set of built-in tools, collectively called **TensorBoard**, for handling some of this complexity:

https://www.tensorflow.org/tensorboard/graphs

return tf.reduce_sum(tf.square(y_observed - y_predicted))









Option 1: set w and b manually.

We know W=-1, b=1 is the correct answer

Change values of tf.Variables using assign method





Option 1: set w and b manually.

0.0

We know W=-1, b=1 is the correct answer Change values of $t \in V_{0}$ while b = 0 using a set of T_{0}

Change values of tf.Variables using assign method





Option 1: set w and b manually.

We know W=-1, b=1 is the correct answer Change values of tf.Variables using assign method



0.0

Note: because W and b are rank-1 tensors, we have to pass their new values as length-1 lists, not scalars. linear_model.W.assign(-1) would result in an error.



Option 1: set w and b manually.

We know W=-1, b=1 is the correct answer

Change values of tf.Variables using assign method

Option 2: use closed-form solution for loss-minimizing w and b. ...but then what happens when we have a model with no closed-form solution?



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Option 3: take advantage of automatic differentiation Allows easy implementation of gradient descent and related techniques



We know W=-1, b=1 is the correct answer

Change values of tf.Variables using assign method

...but then what

Option 2: use close This is why we use TensorFlow!

w and b.

with no closed-form solution?

Option 3: take advantage of **automatic differentiation** Allows easy implementation of gradient descent and related techniques

Gradient Descent: Crash Course

Iterative optimization method for minimizing a function

At location (w, b), take gradient of loss function with respect to parameters Take a **gradient step** in the direction of the gradient Size of step changes over time according to **learning rate**

Gradient Descent: Crash Course

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At location (w, b), take gradient of loss function with respect to parameters Take a **gradient step** in the direction of the gradient Size of step changes over time according to **learning rate**

In short, gradient descent is a method for minimizing a function, provided we can compute its gradient (i.e., derivative). It's enough for this course to treat this as a black box.

For more information:

S. P. Boyd and L. Vandenberghe (2004). *Convex Optimization*. Cambridge University Press. J. Nocedal and S. J. Wright (2006). *Numerical Optimization*. Springer.



Define a train function, which takes a single gradient step with respect to a model's performance with respect to a loss function on data x and y, with a given learning rate.



The tf.GradientTape object keeps track of our gradients. This is especially useful when we want to check whether or not our estimates have converged. Here, we just need it to do automatic differentiation for us.



model.W.assign_sub(learning_rate*dW)
model.b.assign_sub(learning_rate*db)



Use the tf.GradientTape to compute the gradient of the loss with respect to the current model parameters.

Caution: notice that loss is a Python function, and current_loss is a tf.Tensor that is output by that function. Breaking this pattern is a common source of bugs.

```
def train(model, x, y, learning_rate):
    with tf.GradientTape() as t:
        current_loss = loss(y, model(x))
    (dW, db) = t.gradient(current_loss, [model.W, model.b])
    model.W.assign_sub( learning_rate*dW )
    model.b.assign_sub( learning_rate*db )
    Update the parameters. assign_sub is the
    tf.Variable analogue of writing x = x-dx.
```

```
def train(model, x, y, learning rate):
   with tf.GradientTape() as t:
        current loss = loss(y, model(x))
    (dW, db) = t.gradient(current loss, [model.W, model.b])
   model.W.assign sub( learning rate*dW )
   model.b.assign sub( learning rate*db )
x = tf.constant([1,2,3,4], dtype=tf.float32)
                                                     Initialize the model parameters randomly.
y = tf.constant( [0,-1,-2,-3], dtype=tf.float32 )
                                                     tf.random.normal is similar to numpy/scipy
                                                     RNGs. Note that we need our random variables to
linear model.W.assign(tf.random.normal(shape=[1]))
                                                     be shape=[1] to match the shapes of W and b.
linear model.b.assign(tf.random.normal(shape=[1]))
(linear model.W.numpy(), linear model.b.numpy())
```

(array([-0.49148715], dtype=float32), array([0.48135814], dtype=float32))

```
def train(model, x, y, learning_rate):
    with tf.GradientTape() as t:
        current_loss = loss(y, model(x))
    (dW, db) = t.gradient(current_loss, [model.W, model.b])
    model.W.assign sub( learning rate*dW )
```

model.b.assign_sub(learning_rate*dw)
model.b.assign_sub(learning_rate*db)

```
x = tf.constant( [1,2,3,4], dtype=tf.float32 )
y = tf.constant( [0,-1,-2,-3], dtype=tf.float32 )
```

```
linear_model.W.assign(tf.random.normal(shape=[1]))
linear_model.b.assign(tf.random.normal(shape=[1]))
(linear_model.W.numpy(), linear_model.b.numpy())
```

(array([-0.49148715], dtype=float32), array([0.48135814], dtype=f]

for i in range(1000):
 train(linear_model, x, y, learning_rate=0.01) 1
(linear_model.W.numpy(), linear_model.b.numpy())

Each iteration of this loop computes one gradient step and updates the variables accordingly.

(array([-0.9999991], dtype=float32), array([0.99999744], dtype=float32))

```
x = tf.constant( [1,2,3,4], dtype=tf.float32 )
y = tf.constant( [0,-1,-2,-3], dtype=tf.float32 )
linear_model.W.assign([0.5])
linear_model.b.assign([-0.5])
(linear_model.W.numpy(), linear_model.b.numpy())
losses = list(range(1000))
for i in range(1000):
    train(linear_model, x, y, learning_rate=0.01)
    losses[i] = loss(linear_model(x), y)
plt.xlabel('step'); plt.ylabel('loss'); = plt.plot(losses);
```



Note: TensorBoard includes a set of tools for visualization, including for tracking loss, but the approach here is quicker and easier for our purposes.
TensorFlow Estimators API: tf.estimators

tf.estimators is a TF module that simplifies model training and evaluation

Module allows one to run models on CPU or GPU, local or on GCP, etc

Simplifies much of the work of building the graph and estimating parameters

More information:

https://www.tensorflow.org/guide/estimator

Note: Keras in TensorFlow v2 serves similar purpose for specifying neural nets <u>https://www.tensorflow.org/guide/keras</u>