

## Multivariate cortical shape modeling based on sparse representation

### Abstract No:

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### Introduction:

A shape representation is an important problem to understand brain morphological changes related to illness or disease. We represent a new shape representation method using the eigenfunctions of Laplace-Beltrami (LB) operator. Since the LB-eigenfunctions reflect the intrinsic geometry of the surfaces, cortical surfaces can be intrinsically represented as a Fourier series expansion using the LB-eigenfunctions [4]. However, some coefficients may not necessarily contribute significantly in reconstructing the surfaces. Thus, we aim to find an optimal sparse solution for the Fourier expansion using an  $l_1$ -penalty. By doing so, we can avoid surface smoothing [1,2,5] that reduces statistical power. We applied this sparse representation in detecting abnormal local shape variations in autism via multivariate general linear modeling [2].

### Methods:

#### Data:

We obtained 3-T brain MRI data for 16 high functioning autistic and 11 control right-handed males, with average ages of  $17.18 \pm 2.89$  and  $16.13 \pm 4.51$  respectively. After a sequence of image processing steps, outer cortical surfaces are extracted as triangular mesh with  $n=40,962$  vertices via deformable surface modeling [1] which establishes a surface correspondence across all the surfaces.

#### Fourier Analysis:

The eigenfunctions  $\Psi_j$  of the LB operator  $\Delta$  on a cortical manifold, i.e.

$$\Delta\Psi_j = -\lambda_j\Psi_j,$$

form an orthonormal basis for the space of square integrable functions on the manifold. Taking surface coordinates as functions to be estimated, the

coordinates can be represented as a linear combination of the LB-eigenfunctions. Firstly, we construct a template cortical surface by averaging coordinates of corresponding mesh vertices. Then, the LB-eigenfunctions are computed on the template mesh using the Cotan formulation [4,5]; Fig. 1 shows few representative eigenfunctions. The MATLAB code is given at <http://brainimaging.waisman.wisc.edu/~chung/lb>. The Fourier coefficients can be obtained from the least squares estimation (LSE) by solving the system of linear equations

$$p_i = \Psi\beta,$$

where  $p_i$  is the  $i$ -th coordinate vector,  $\Psi$  is a matrix having LB-eigenfunctions as columns, and  $\beta$  is the Fourier coefficient vector. Fig. 2 blue line shows absolute value of the coefficients estimated by the LSE with first 7396 eigenfunctions for one particular coordinate.

**Sparse representation:**

We can get a more compact and sparse representation than LSE by assuming some of coefficients are not contributing significantly. This is achieved by solving the following  $l_1$ -norm regularization problem [3]:

$$\min (\| p_i - \Psi\beta \|_2)^2 + \lambda \| \beta \|_1.$$

The parameter  $\lambda$  controls the sparsity, and we empirically selected  $\lambda=10$  leading to sufficient sparsity (Fig. 2 red line); in average, 1100 nonzero elements out of 7396 remain.

**Multivariate general linear model:**

To localize shape difference between the groups, we used a multivariate linear model [2]:

$$[ p_1 \ p_2 \ p_3 ] = B_0 + \text{age} B_1 + \text{group} B_2 + \text{age} \cdot \text{group} B_3.$$

### **Results:**

We have tested the group effect ( $B_2$ ) while accounting for age effect, but could not detect any shape difference between autistic and control groups at  $\alpha = 0.1$  level (corrected). However, for an interaction between age and group ( $B_3$ ), we detected the regions where the rate of local shape variation is different (Fig. 3a). Fig. 4 shows regression plots at the most significant vertex ( $\max F = 67.31$ , corrected  $p = 0.006$ , Fig. 3a arrow) in the left prefrontal cortical region. With the LSE (Fig. 3b), we have observed similar results but with less smoothing ( $\max F = 79.38$ ,  $p = 0.005$ ).

### **Conclusions:**

The proposed sparse shape representation demonstrates its potential for

modeling cortical shape variations without using surface-based smoothing that reduces statistical power unnecessarily.

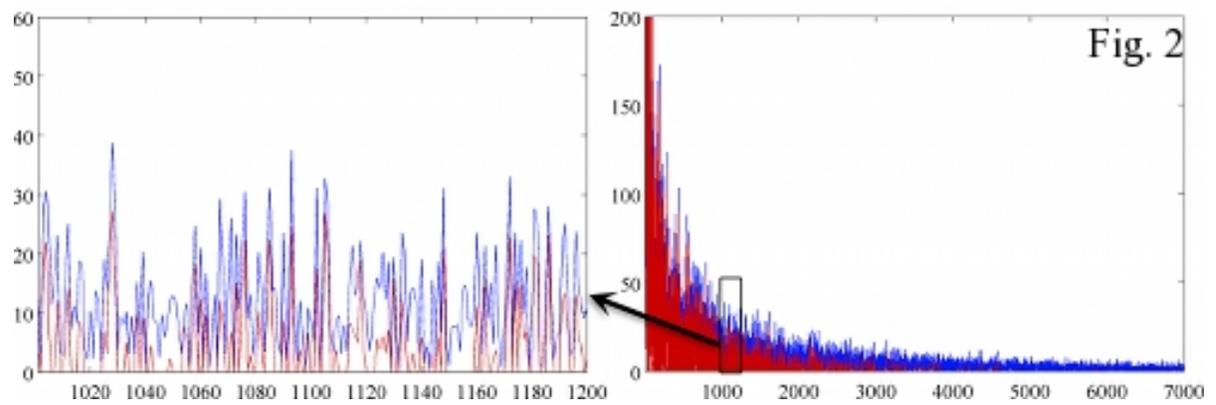
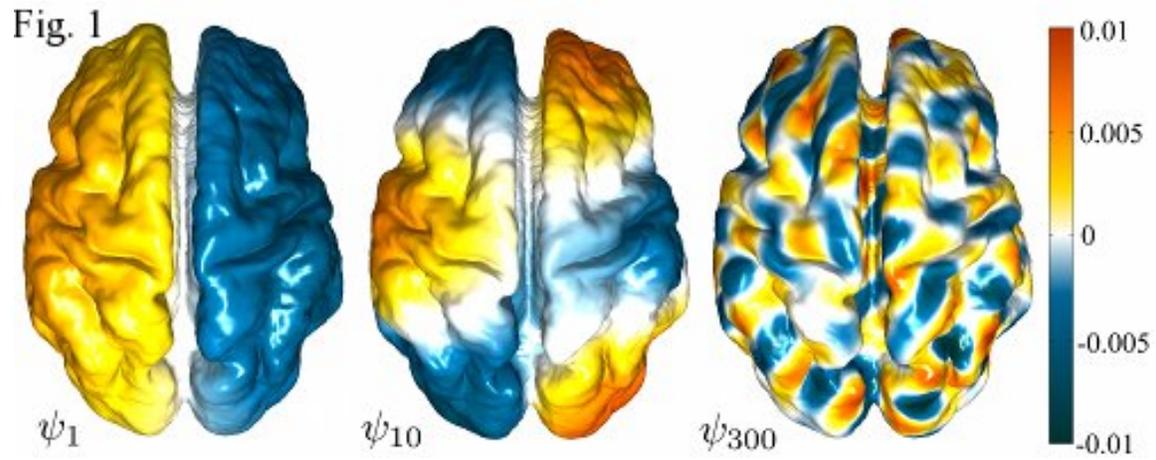


Fig. 3a

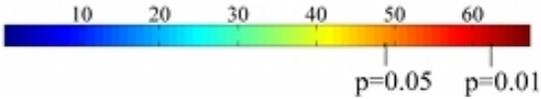
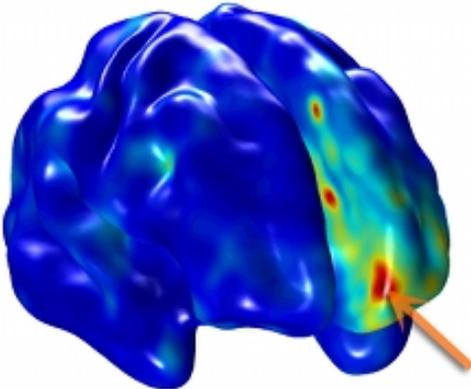
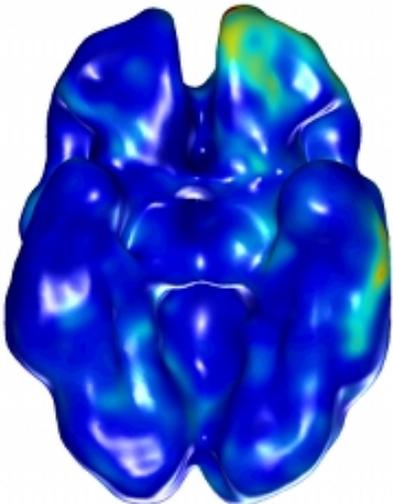
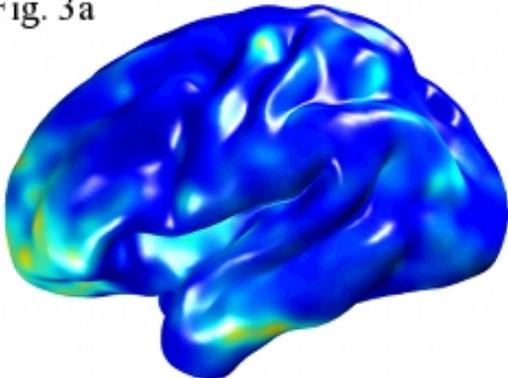


Fig. 3b

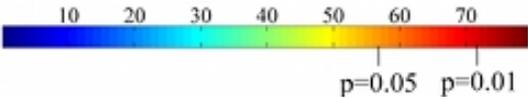
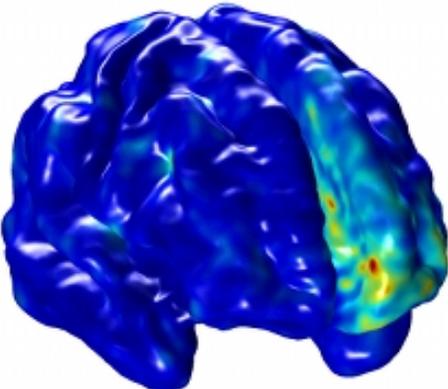
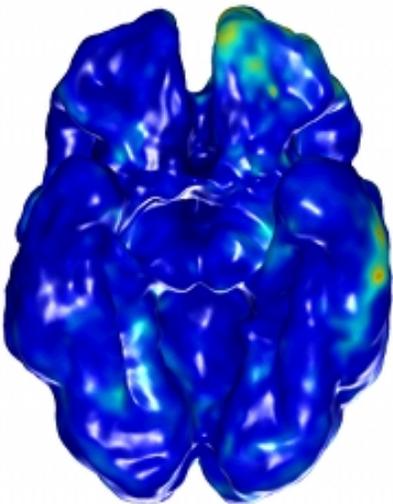
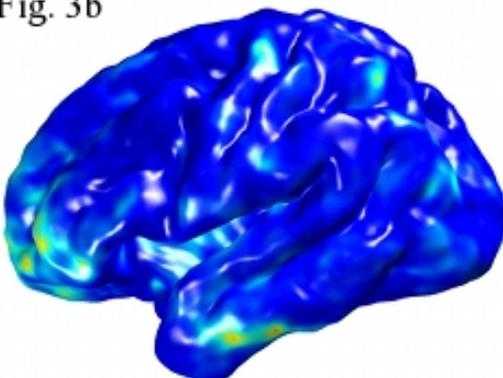
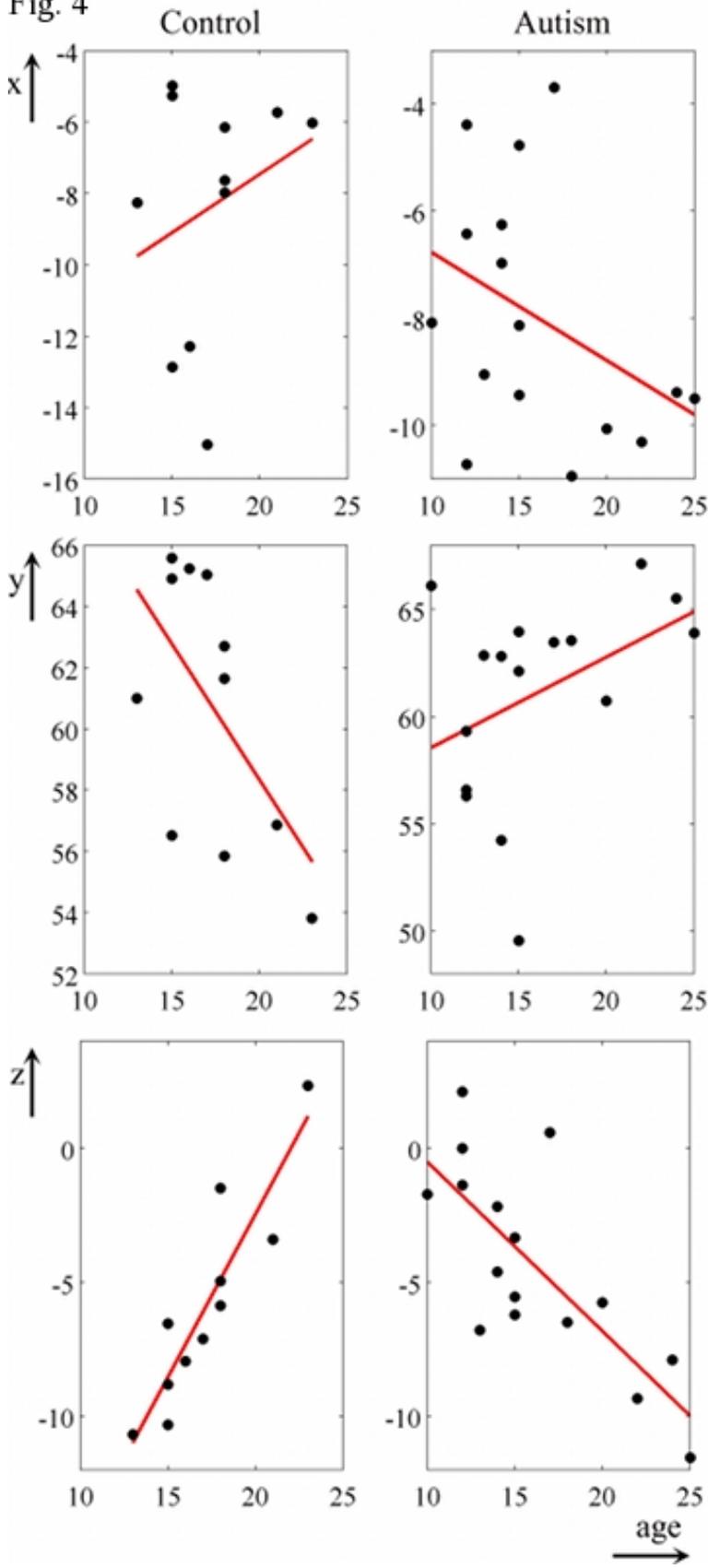


Fig. 4



## References:

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## Modeling and Analysis Methods

Multivariate Modeling