## Assignment #6 — Due Friday, October 28 by 4:00 P.M.

Turn in homework to your TA's mailbox using this sheet as the cover page.

Fill in your name and also circle the *lecture section in which you are registered* and circle the *discussion section* you expect to attend to pick up this assignment.

Name:

Lecture 1 (Hanlon).	<b>311:</b> Tu 1:00 - 2:15pm	<b>312:</b> Th 8:00 - 9:15am	<b>313:</b> We 1:00 - 2:15pm
Lecture 2 (Larget).	<b>321:</b> Tu 1:00 - 2:15pm	<b>322:</b> We 2:30 - 3:45pm	<b>323:</b> We 1:00 - 2:15pm

Please answer the following questions.

- 1. Let  $Z \sim N(0,1)$ . Answer the following questions using *both* the normal table and software (such as R).
  - (a) Compute  $\mathsf{P}(Z \le 0.75)$ .
  - (b) Compute  $P(Z \ge -0.97)$ .
  - (c) Compute  $P(-1.18 \le Z \le -1.11)$ .
  - (d)  $\mathsf{P}(Z > z) = 0.05$ . Find z.
  - (e)  $\mathsf{P}(Z < z) = 0.10$ . Find z.
  - (f) P(-z < Z < z) = 0.7. Find z.
- 2. Let t(x) denote a t random variable with x degrees of freedom. Answer the following questions using both the t table and software (such as R).
  - (a) Let  $T \sim t(10)$ . Compute  $\mathsf{P}(T \leq 0.75)$ .
  - (b) Let  $T \sim t(13)$ . Compute  $\mathsf{P}(T \ge -0.97)$ .
  - (c) Let  $T \sim t(19)$ . Compute  $\mathsf{P}(-1.18 \le T \le -1.11)$ .
  - (d) Let  $T \sim t(11)$ .  $\mathsf{P}(T > z) = 0.05$ . Find z.
  - (e) Let  $T \sim t(15)$ .  $\mathsf{P}(T < z) = 0.10$ . Find z.
  - (f) Let  $T \sim t(17)$ .  $\mathsf{P}(-z < T < z) = 0.7$ . Find z.
- 3. The total nitrogen concentration of the blood plasma of healthy 40 day old albino rats is normally distributed with mean 1.25 g/100ml and standard deviation 0.0080 g/100ml. Let  $\bar{X}$  represent the mean nitrogen concentration level of 25 rats randomly chosen from this population.
  - (a) If a healthy 40 day old albino rat is chosen at random, what is the probability that the total nitrogen concentration of its blood plasma will be between 1.26 g/100 ml and 1.30 g/100 ml?
  - (b) What is the value of nitrogen concentration such that 65% of 40 day old albino rats have a nitrogen concentration higher than that value?
  - (c) Compute  $P(1.24 \le \bar{X} \le 1.26)$
  - (d) Compute the 0.90 quantile of the sampling distribution of  $\bar{X}$ .
  - (e) Compute the cutoff values for the middle 80% of the sampling distribution of  $\bar{X}$ .
- 4. Textbook p.254, Problem 16
- 5. Textbook p.254, Problem 17
- 6. Textbook p.255, Problem 20