

STATS 507

Data Analysis in Python

Lecture 3: Lists

Python Lists

Strings in Python are “sequences of characters”

But what if I want a sequence of something else?

A vector would be naturally represented as a sequence of numbers

A class roster might be represented as a sequence of strings

Python lists are sequences whose values can be of any data type

We call these list entries the **elements** of the list

Constructing Lists

We create a list by putting its elements between square brackets, separated by commas.

```
1 fruits = ['apple', 'orange', 'banana', 'kiwi']
2 fibonacci = [0, 1, 1, 2, 3, 5, 8, 13, 21]
3 mixed = ['one', 2, 3.0]
4 pythagoras = [[3, 4, 5], [5, 12, 13], [8, 15, 17]]
```

Constructing Lists

We create a list by putting its elements between square brackets, separated by commas.

This is a list of four strings.


```
1 fruits = ['apple', 'orange', 'banana', 'kiwi']  
2 fibonaccis = [0, 1, 1, 2, 3, 5, 8, 13, 21]  
3 mixed = ['one', 2, 3.0]  
4 pythagoras = [[3, 4, 5], [5, 12, 13], [8, 15, 17]]
```

Constructing Lists

We create a list by putting its elements between square brackets, separated by commas.

```
1 fruits = ['apple', 'orange', 'banana', 'kiwi']  
2 fibonacci = [0, 1, 1, 2, 3, 5, 8, 13, 21]  
3 mixed = ['a', 8, 3.0]  
4 pythagoras = [[3, 4, 5], [5, 12, 13], [8, 15, 17]]
```

This is a list of nine integers



Constructing Lists

We create a list by putting its elements between square brackets, separated by commas.

```
1 fruits = ['apple', 'orange', 'banana', 'kiwi']
2 fibonacci = [0, 1, 1, 2, 3, 5, 8, 13, 21]
3 mixed = ['one', 2, 3.0]
4 pythagoras = [(3, 4, 5), (5, 12, 13), (8, 15, 17)]
```

The elements of a list need not be of the same type. Here is a list with a string, an integer and a float.

Constructing Lists

We create a list by putting its elements between square brackets, separated by commas.

```
1 fruits = ['apple', 'orange', 'banana', 'kiwi']
2 fibonacci = [0, 1, 1, 2, 3, 5, 8, 13, 21]
3 mixed = ['one', 2, 3.0]
4 pythagoras = [[3, 4, 5], [5, 12, 13], [8, 15, 17]]
```

A list can even contain more lists!
This is a list of three lists, each of which is a list of three integers.

Constructing Lists

It is possible to construct a list with no elements, the empty list.

```
1 x = []  
2 x
```

```
[]
```

```
1 x = list()  
2 x
```

```
[]
```

Two equivalent ways of creating an empty list.

Straight-forwardly create a list using square brackets notation, but supply no elements. So `x` is empty.

Use the reserved keyword `list`, which casts to a list. Given no arguments, it creates an empty list.

Accessing List Elements

```
1 fruits = ['apple', 'orange', 'banana', 'kiwi']  
2 fruits[0]
```

'apple'

```
1 fruits[1]
```

'orange'

```
1 fruits[2]
```

'banana'

```
1 fruits[-1]
```

'kiwi'

We can access individual elements of a list just like a string. This is because both strings and lists are examples of Python **sequences**.

Indexing from the end of the list, just like with strings.

Accessing List Elements

```
1 fruits = ['apple', 'orange', 'banana', 'kiwi']
2 fruits
```

```
['apple', 'orange', 'banana', 'kiwi']
```

Unlike strings, lists are **mutable**. We can change individual elements after creating the list.

```
1 fruits[-1] = 'mango'
2 fruits
```

```
['apple', 'orange', 'banana', 'mango']
```

Reminder of what happens if we try to do this with a string. This error is because strings are **immutable**. Once they're created, they can't be altered.

```
1 mystring = 'goat'
2 mystring[0]='b'
```

TypeError

Traceback (most recent call last)

<ipython-input-86-b526da741b9a> in <module>()

```
1 mystring = 'goat'
```

```
----> 2 mystring[0]='b'
```

TypeError: 'str' object does not support item assignment

Lists are sequences, so they have a length

```
1 fruits = ['apple', 'orange', 'banana', 'kiwi']  
2 len(fruits)
```

4

```
1 len([])
```

The empty list has length 0, just like the empty string.

0

```
1 pythagoras = [[3, 4, 5], [5, 12, 13], [8, 15, 17]]  
2 len(pythagoras)
```

3

One might be tempted to say that `pythagoras` should have length 9, but each element of a list counts only once, even if it is itself a more complicated object!

Lists are sequences, so they support the `in` operator

```
1 fruits = ['apple', 'orange', 'banana', 'kiwi']  
2 'apple' in fruits
```

True

Just like with strings, `x in y` returns True if and only if `x` is an element of `y`.

```
1 'grape' in fruits
```

False

```
1 ['apple', 'orange'] in fruits
```

False

Warning: This contrasts with the string case. Recall that `'ap' in 'apple'` evaluates to True. By analogy, this line of code should also evaluate to True, but it doesn't, because for lists, the `in` operator only checks elements, not subsequences.

```
1 ['cat', 'dog'] in [['cat', 'dog'], ['bird', 'goat']]
```

True

Common pattern: list traversal

For each element of a list, do something with that element

```
1 fruits = ['apple', 'orange', 'banana', 'kiwi']
2 for f in fruits:
3     print(f)
```

```
apple
orange
banana
kiwi
```

```
1 numbers = range(5)
2 for n in numbers:
3     print(2**n)
```

```
1
2
4
8
16
```

`range(x)` produces a list of the integers 0 to $x-1$.

For more information:

<https://docs.python.org/3/library/stdtypes.html#ranges>

Common pattern: list traversal

For each element of a list, do something with that element

```
1 fruits = ['apple', 'orange', 'banana', 'kiwi']
2 for i in range(len(fruits)):
3     fruits[i] = fruits[i].upper()
4
5 for f in fruits:
6     print(f)
```

Sometimes, we need to be able to index into the list itself, in which case we use a slightly different traversal pattern, in which we iterate an **index variable**, `i` in this example.

```
APPLE
ORANGE
BANANA
KIWI
```

Common pattern: list traversal

For each element of a list, do something with that element

```
1 fruits = ['apple', 'orange', 'banana', 'kiwi']
2 for i in range(len(fruits)):
3     fruits[i] = fruits[i].upper()
4
5 for f in fruits:
6     print(f)
```

Sometimes, we need to be able to index into the list itself, in which case we use a slightly different traversal pattern, in which we iterate an **index variable**, `i` in this example.

APPLE
ORANGE
BANANA
KIWI

Note: this operation is possible because lists are mutable!

List operations: concatenation

List concatenation is similar to strings.

```
1 fibonacci = [0,1,1,2,3,5,8]
2 primes = [2,3,5,7,11,13]
3 fibonacci + primes
```

```
[0, 1, 1, 2, 3, 5, 8, 2, 3, 5, 7, 11, 13]
```

```
1 3*['cat', 'dog']
```

```
['cat', 'dog', 'cat', 'dog', 'cat', 'dog']
```

These operations are precisely analogous to the corresponding string operations. This makes sense, since both strings and lists are **sequences**.

<https://docs.python.org/3/library/stdtypes.html#typeseq>

List operations: slices

Also like strings, it is possible to select **slices** of a list

```
1 animals = ['cat', 'dog', 'goat', 'bird', 'llama']  
2 animals[1:3]
```

```
['dog', 'goat']
```

```
1 animals[3:]
```

```
['bird', 'llama']
```

Again, analogously to the corresponding string operations.
<https://docs.python.org/3/library/stdtypes.html#typeseq>

```
1 animals[:2]
```

```
['cat', 'dog']
```

```
1 animals[:]
```

```
['cat', 'dog', 'goat', 'bird', 'llama']
```

List Methods

Lists supply a certain set of methods:

`list.append(x)`: adds `x` to the end of the list

`list.extend(L2)`: adds list `L2` to the end of another list (like concatenation)

`list.sort()`: sort the elements of the list

`list.remove(x)`: removes from the list the first element equal to `x`.

`list.pop()`: removes the last element of the list and returns that element.

`list.append()` and `list.extend()`

```
1 animals = ['cat', 'dog', 'goat', 'bird']
2 animals.append('unicorn')
3 animals
```

```
['cat', 'dog', 'goat', 'bird', 'unicorn']
```

We call list methods with dot notation. These are **methods** supported by certain **objects**.

```
1 fibonacci = [0,1,1,2,3,5,8]
2 fibonacci.append([13,21])
3 fibonacci
```

```
[0, 1, 1, 2, 3, 5, 8, [13, 21]]
```

Warning: `list.append()` adds its argument as the last element of a list! Use `list.extend()` to concatenate to the end of the list!

```
1 fibonacci = [0,1,1,2,3,5,8]
2 fibonacci.extend([13, 21])
3 fibonacci
```

```
[0, 1, 1, 2, 3, 5, 8, 13, 21]
```

Note: all of these list methods act upon the list that calls the method. These methods don't return the new list, they alter the list on which we call them.

list.sort() and sorted()

```
1 animals = ['cat', 'dog', 'goat', 'bird']  
2 animals.sort()  
3 animals
```

```
['bird', 'cat', 'dog', 'goat']
```

```
1 mixed = [1, 'two', 3.0, [4,5]]  
2 mixed.sort()  
3 mixed
```

```
[1, 3.0, [4, 5], 'two']
```

```
1 animals = ['cat', 'dog', 'goat', 'bird']  
2 sorted_animals = sorted(animals)  
3 sorted_animals
```

```
['bird', 'cat', 'dog', 'goat']
```

```
1 animals
```

```
['cat', 'dog', 'goat', 'bird']
```

`list.sort()` sorts the list **in place**. See documentation for how Python sorts data of different types.

If I don't want to sort a list in place, the `sorted()` command returns a sorted version of the list, leaving its argument unchanged.

Removing elements: `list.pop()`

```
1 animals = ['cat', 'dog', 'goat', 'bird']  
2 animals.pop()
```

'bird'

`list.pop()` removes the last element from the list and returns that element.

```
1 animals
```

['cat', 'dog', 'goat']

```
1 fibonacci = [0,1,1,2,3,5,8]  
2 fibonacci.pop(3)
```

`list.pop()` takes an **optional argument**, which indexes into the list and removes and returns the indexed element

2

```
1 fibonacci
```

[0, 1, 1, 3, 5, 8]

Again, this method alters the list itself, rather than returning an altered list.

Removing elements: `list.remove()`

```
1 animals = ['cat', 'dog', 'goat', 'bird']
2 animals.remove('cat')
3 animals
```

```
['dog', 'goat', 'bird']
```

```
1 numbers = [0,1,2,3,1,2,3,2,3]
2 numbers.remove(2)
3 numbers
```

```
[0, 1, 3, 1, 2, 3, 2, 3]
```

```
1 numbers.remove(4)
```

`list.remove(x)` removes the first instance of `x` in the list.

Raises a `ValueError` if no such element exists.

ValueError

Traceback (most recent call last)

```
<ipython-input-160-6d289ee6c03d> in <module>()
```

```
----> 1 numbers.remove(4)
```

ValueError: list.remove(x): x not in list

Map, filter and reduce

Example: suppose I want to square every element of a list.

```
1 def square_all(t):  
2     res = []  
3     for elmt in t:  
4         res.append(elmt**2)  
5     return res  
6  
7 square_all(range(10))
```

```
[0, 1, 4, 9, 16, 25, 36, 49, 64, 81]
```

```
1 fibonacci = [0,1,1,2,3,5,8,13,21]  
2 square_all(fibonacci)
```

```
[0, 1, 1, 4, 9, 25, 64, 169, 441]
```

```
1 fibonacci
```

```
[0, 1, 1, 2, 3, 5, 8, 13, 21]
```

This function takes a list `t`, and creates a new list `res`, which consists of the squares of the elements of `t`.

This kind of operation, in which we apply a function to each element of a list, is called a **map** operation.

Note: unlike the list methods in the previous slides, this function creates a new list, and doesn't alter the argument.

Map, filter and reduce

Example: I want to remove all even numbers from a list.

```
1 def remove_even(t):
2     res = []
3     for elmt in t:
4         if elmt % 2 == 0:
5             continue
6         else: # elmt is odd.
7             res.append(elmt)
8     return res
9
10 remove_even(range(10))
```

```
[1, 3, 5, 7, 9]
```

```
1 fibonacci = [0,1,1,2,3,5,8,13,21]
2 remove_even(fibonacci)
```

```
[1, 1, 3, 5, 13, 21]
```

```
1 fibonacci
```

```
[0, 1, 1, 2, 3, 5, 8, 13, 21]
```

This function takes a list `t`, and creates a new list `res`, which contains only the odd elements of `t`.

This kind of operation, in which we keep only the elements of a list that satisfy some condition, is called a **filter** operation.

Note: again, this function creates a new list, and doesn't alter the argument.

Map, filter and reduce

Example: compute the sum of a list of numbers

```
1 def my_sum(t):
2     res = 0
3     for elmt in t:
4         res += elmt
5     return res
6
7 my_sum(range(10))
```

This function takes a list `t`, sums the elements of `t`, and returns the sum.

This notation may be familiar to you already. It is called **augmented assignment**. It is short for `res = res + elmt`.

The variable `res` holds a running sum. We call a variable like this an **accumulator**.

This kind of operation, in which we combine the elements of a list to obtain a single element, is called a **reduce** operation.

45

```
1 fibonacci = [0,1,1,2,3,5,8,13,21]
2 my_sum(fibonacci)
```

54

```
1 my_sum([])
```

0

Map, filter and reduce

We'll see lots more of these operations later in the course

They're fundamental to functional programming

MapReduce and related frameworks are built on this paradigm

Note: all examples were on lists of numbers...

...but can write similar functions for strings or other more complicated data

Some of these operations can be expressed with Python **list comprehensions**

Map with list comprehensions

Basic pattern: `[f(x) for x in mylist]`
creates a new list, whose elements are the
elements of `mylist`, each with function `f` applied.

```
1 zero2nine = range(10)
2 [x**2 for x in zero2nine]
```

```
[0, 1, 4, 9, 16, 25, 36, 49, 64, 81]
```

```
1 animals = ['cat', 'dog', 'goat', 'bird']
2 [s.upper() for s in animals]
```

```
['CAT', 'DOG', 'GOAT', 'BIRD']
```

Note: the function `f` must
actually return something!

List comprehensions are a special pattern
supplied by Python. They're one of the
features of Python that makes it appealing.
Very expressive way to write operations!

Filter with list comprehensions

```
1 fibonacci = [0,1,1,2,3,5,8,13,21]
2 [x for x in fibonacci if x % 2 == 1]
```

```
[1, 1, 3, 5, 13, 21]
```

```
1 animals = ['cat', 'dog', 'goat', 'bird']
2 [x.upper() for x in animals if 'o' in x[1]]
```

```
['DOG', 'GOAT']
```

```
1 [x for x in animals if len(x)==5]
```

```
[]
```

Basic pattern:

`[x for x in mylist if boolean_expr]`
creates a new list of all and only the elements of
mylist that satisfy `boolean_expr`.

Can combine filter and map to
apply a function to only the
elements that pass the filter.

Lists and strings

Lists and strings are both sequences, but they aren't quite the same...

```
1 goatstr = 'goat'  
2 goatlist = list(goatstr)  
3 goatlist
```

```
['g', 'o', 'a', 't']
```

`str.split()` turns a string into a list of strings, splitting the string on its argument, called the **delimiter**.

```
1 wittgenstein = 'Die Welt ist alles was der Fall ist.'  
2 t = wittgenstein.split(' ')  
3 t
```

```
['Die', 'Welt', 'ist', 'alles', 'was', 'der', 'Fall', 'ist.']
```

```
1 delim = ' '  
2 delim.join(t)
```

`str.join()` is like the inverse of `str.split()`. It takes a list of strings and joins them into a single string.

```
'Die Welt ist alles was der Fall ist.'
```

Equivalent vs identical objects

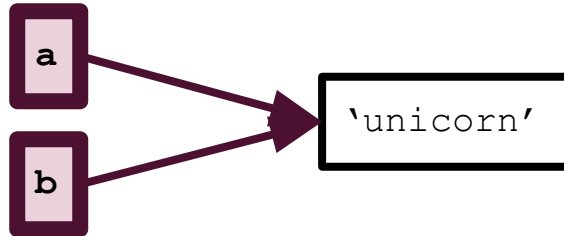
```
1 a = 'unicorn'  
2 b = 'unicorn'
```

Question: are a and b the same?

Well, what do we mean by “the same”?

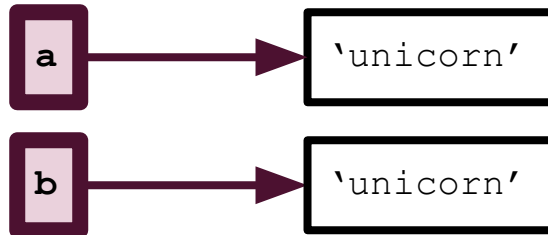
Possibility 1:

a and b both ‘point to’
the *same* object.



Possibility 2:

a and b ‘point to’ different
objects, both objects have
same value.



Equivalent vs identical objects

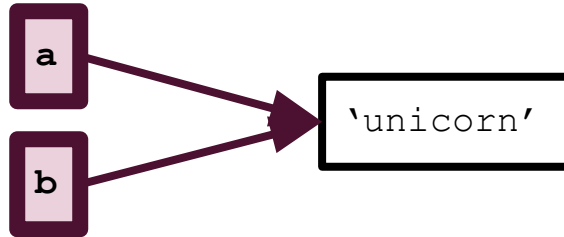
```
1 a = 'unicorn'  
2 b = 'unicorn'
```

Question: are a and b the same?

Well, what do we mean by “the same”?

Possibility 1:

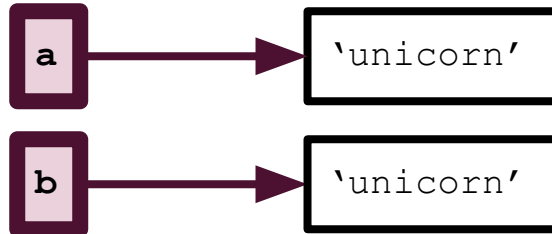
a and b both ‘point to’ the *same* object.



In this case, we say that a and b are **identical**

Possibility 2:

a and b ‘point to’ different objects, both objects have *same value*.



In this case, we say that a and b are **equivalent**

Equivalent vs identical objects

```
1 a = 'unicorn'  
2 b = 'unicorn'
```

```
1 a == b
```

True

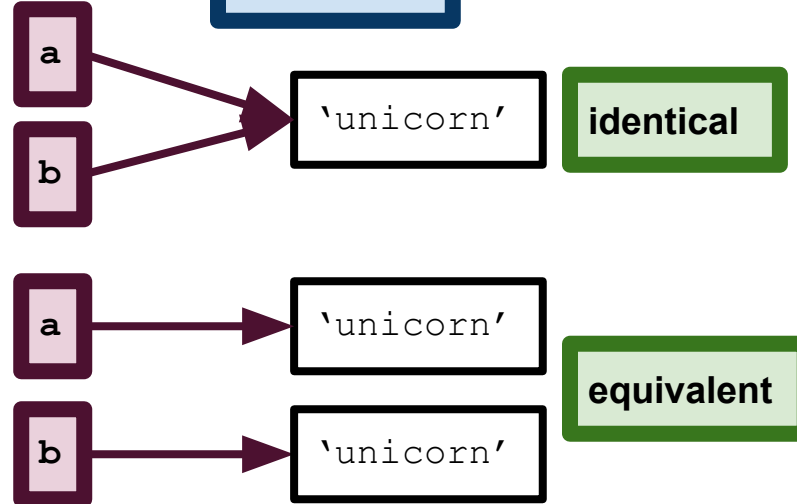
```
1 a is b
```

True

`==` tests if two variables are **equivalent**.
`is` tests if two variables are **identical**.

Strings are immutable, so Python only creates one copy of the string `'unicorn'`, and both `a` and `b` point to it. So they are equivalent **and** identical.

Reminder:



Equivalent vs identical objects

```
1 a = [1,2,3]
2 b = [1,2,3]
3 a == b
```

True

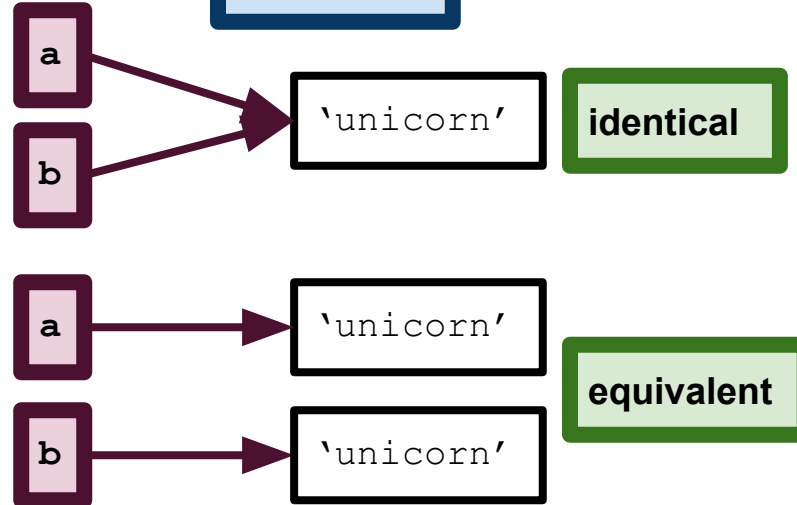
```
1 a is b
```

False

`==` tests if two variables are **equivalent**.
`is` tests if two variables are **identical**.

Lists are mutable, so Python creates different copies for `a` and `b`. So they are equivalent but **not** identical.

Reminder:

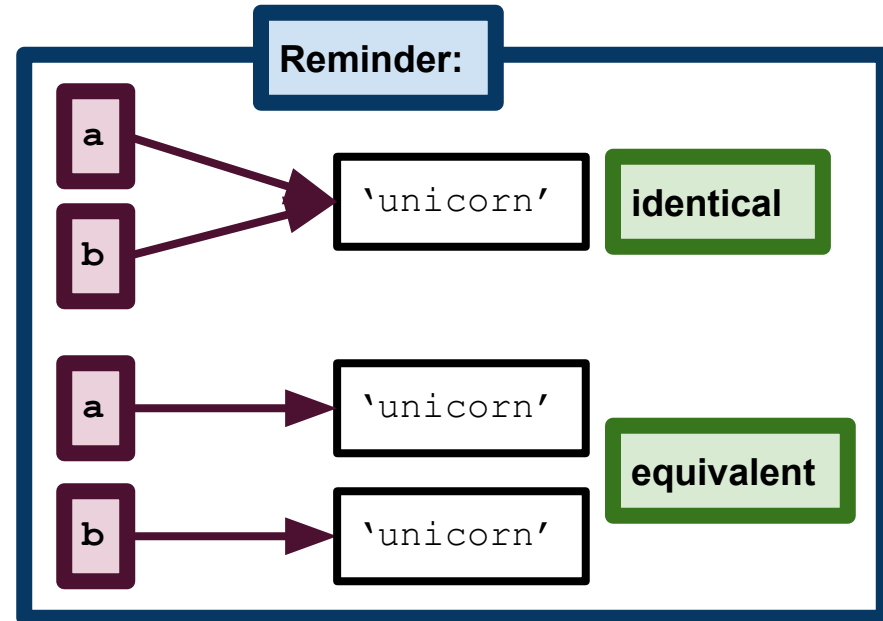


Equivalent vs identical objects: reference

```
1 a = [1,2,3]
2 b = a
3 a is b
```

`==` tests if two variables are **equivalent**.
`is` tests if two variables are **identical**.

Question: will this evaluate to `True` or `False`?



Equivalent vs identical objects: reference

```
1 a = [1,2,3]
2 b = a
3 a is b
```

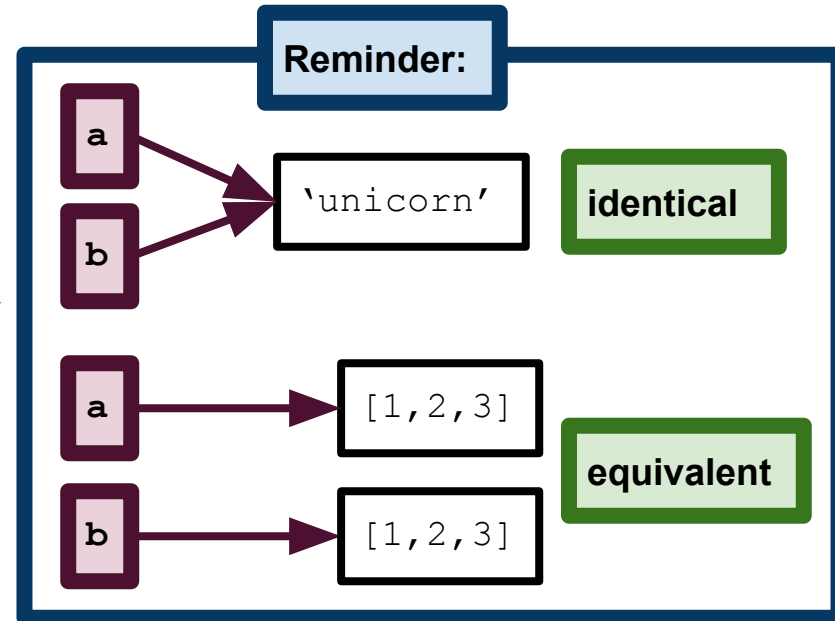
True

Answer: evaluates to `True`, because assignment changes the **reference** of a variable.

Reference of a variable is the value to which it “points”, like on the right.

An object that has more than one reference (i.e., more than one “name”) is called **aliased**. So, on the right, `'unicorn'` is aliased.

`==` tests if two variables are **equivalent**.
`is` tests if two variables are **identical**.



Equivalent vs identical objects: reference

```
1 a = [1, 2, 3]
2 b = a
3 b[-1] = 42
4 b
```

```
[1, 2, 42]
```

```
1 a[-1]
```

Warning: Aliased mutable objects can sometimes cause unexpected behavior.

Question: what should this evaluate to?

Equivalent vs identical objects: reference

```
1 a = [1, 2, 3]
2 b = a
3 b[-1] = 42
4 b
```

```
[1, 2, 42]
```

```
1 a[-1]
```

```
42
```

Warning: Aliased mutable objects can sometimes cause unexpected behavior.

Question: what should this evaluate to?

Answer: when we changed the last element of `b`, we changed the object referenced by both `a` and `b`.

Pass-by-reference vs pass-by-value

```
1 def make_end_42(t):  
2     # Change the last element of  
3     # list t to be 42.  
4     t[-1] = 42  
5  
6 a = [1,2,3]  
7 make_end_42(a)  
8 a
```

[1, 2, 42]

When you pass an object to a function, the function gets a reference to that object. So changes that we make inside the function are also true outside. This is called **pass-by-reference**, because the function gets a reference to its argument.

Note: strictly speaking, what Python does is not pass-by-reference in the same way as what is normally meant by the term. This is because Python does not use pointers per se in the way that, e.g., C/C++ does.

Pass-by-reference vs pass-by-value

```
1 def wrong_make_end_42(t):
2     # Change the last element of
3     # list t to be 42, incorrectly.
4     t = t[:-1] # delete the last element.
5     t.append(42)
6
7 a = [1,2,3]
8 wrong_make_end_42(a)
9 a
```

When we make the assignment to `t`, we create a new list, and the reference of `t` is changed, so it no longer points to the list that we passed to the function!

[1, 2, 3]

Moral of the story: be careful when working with mutable objects, especially when you are trying to modify objects in place. Often, it's better to just write a function that modifies a list and returns the modified list!