STATS 701
Data Analysis using Python
Lecture 4: Dictionaries
Two more fundamental build-in data structures

Dictionaries
- Python dictionaries generalize lists
- Allow indexing by arbitrary immutable objects rather than integers
- Fast lookup and retrieval
  https://docs.python.org/3/tutorial/datastructures.html#dictionaries

Tuples
- Similar to a list, in that it is a sequence of values
- But unlike lists, tuples are immutable
  https://docs.python.org/3/tutorial/datastructures.html#tuples-and-sequences
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Generalized lists: Python `dict()`

Python dictionary generalizes lists
- `list()`: indexed by integers
- `dict()`: indexed by (almost) any data type

Dictionary contains:
- a set of indices, called `keys`
- A set of values (called `values`, shockingly)

Each key associated with one (and only one) value
- `key-value pairs`, sometimes called `items`
- Like a function $f$: keys $\rightarrow$ values
Dictionary maps keys to values.

E.g., ‘cat’ mapped to the float 2.718

Of course, the dictionary at the left is kind of silly. In practice, keys are often all of the same type, because they all represent a similar kind of object.

Example: might use a dictionary to map UMich unique names to people
Access the value associated to key \( x \) by \( \text{dictionary}[x] \).
Attempting to access the value associated to a non-existent key results in a KeyError, an error that Python supplies specifically for this situation.

Observe that bird is not a key in this dictionary, so when we try to index with it, we get an error.
Creating and populating a dictionary

Example: University of Mishuges IT wants to store the correspondence between the usernames (UM IDs) of my students to their actual names. A dictionary is a very natural data structure for this.

```
1 umid2name = dict()
2 umid2name['aeinstein'] = 'Albert Einstein'
3 umid2name['kyfan'] = 'Ky Fan'
4 umid2name['enoether'] = 'Emmy Noether'
5 umid2name['cshannon'] = 'Claude Shannon'
```

```
1 umid2name['cshannon']
'Claude Shannon'
```

```
1 umid2name['enoether']
'Amalie Emmy Noether'

1 umid2name['enoether'] = 'Amalie Emmy Noether'
2 umid2name['enoether']
'Amalie Emmy Noether'
```
Creating and populating a dictionary

Create an empty dictionary (i.e., a dictionary with no key-value pairs stored in it. This should look familiar, since it is very similar to list creation.

```python
umid2name = dict()

umid2name['ac einstein'] = 'Albert Einstein'
umid2name['kyfan'] = 'Ky Fan'
umid2name['enoether'] = 'Emmy Noether'
umid2name['cshannon'] = 'Claude Shannon'

umid2name['cshannon']
'Claude Shannon'

umid2name['enoether']
'Emmy Noether'

umid2name['enoether'] = 'Amalie Emmy Noether'
```
Creating and populating a dictionary

Populate the dictionary. We are adding four key-value pairs, corresponding to four users in the system.

```
mid2name = dict()
mid2name['aeinstein'] = 'Albert Einstein'
mid2name['kyfan'] = 'Ky Fan'
mid2name['enoether'] = 'Emmy Noether'
mid2name['cshannon'] = 'Claude Shannon'
```
Creating and populating a dictionary

Retrieve the value associated with a key. This is called **lookup**.
Creating and populating a dictionary

Emmy Noether’s actual legal name was Amalie Emmy Noether, so we have to update her record. Note that updating is, sensibly, no different from initial population of the dictionary.
Displaying Items

Printing a dictionary lists its **items** (key-value pairs), in this rather odd format...

```python
.example_dict
{3.1415: [1, 2, 3], 12: 'one', 'cat': 2.718, 'dog': 2.718, 'goat': 35}
```

...but I can use that format to create a new dictionary.

```python
.umid2name
{'aeinstein': 'Albert Einstein',
 'cshannon': 'Claude Shannon',
 'enoether': 'Amalie Emmy Noether',
 'kyfan': 'Ky Fan'}
```

```python
.umid2name = {'aeinstein': 'Albert Einstein',
 'cshannon': 'Claude Shannon',
 'enoether': 'Amalie Emmy Noether',
 'kyfan': 'Ky Fan'}
```

```python
.umid2name['kyfan']
'Ky Fan'
```

**Note:** the order in which items are printed isn’t always the same, and (usually) isn’t predictable. This is due to how dictionaries are stored in memory. More on this soon.
Dictionaries have a length

Length of a dictionary is just the number of items. Empty dictionary has length 0.

Note: we said earlier than all sequence objects support the length operation. But there exist objects that aren’t sequences that also have this attribute.
Checking set membership

Suppose a new student, Andrey Kolmogorov is enrolling at UMish. We need to give him a unique name, but we want to make sure we aren't assigning a name that's already taken.

Dictionaries support checking whether or not an element is present as a key, similar to how lists support checking whether or not an element is present in the list.
Checking set membership: fast and slow

Lists and dictionaries provide our first example of how certain data structures are better for certain tasks than others.

Example: I have a large collection of phone numbers, and I need to check whether or not a given number appears in the collection. Both dictionaries and lists support membership checks of this sort, but it turns out that dictionaries are much better suited to the job.
Checking set membership: fast and slow

This block of code generates 1000000 random “phone numbers”, and creates (1) a list of all the numbers and (2) a dictionary whose keys are all the numbers.

```python
from random import randint
listlen = 1000000
list_of_numbers = listlen*[0]
dict_of_numbers = dict()
for i in range(listlen):
    n = randint(1000000,9999999)
    list_of_numbers[i] = n
    dict_of_numbers[n] = 1
```

```
8675309 in list_of_numbers
False
```

```
1240893 in list_of_numbers
True
```

```
8675309 in dict_of_numbers
False
```

```
1240893 in dict_of_numbers
True
```
Checking set membership: fast and slow

```python
from random import randint
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    list_of_numbers[i] = n
dict_of_numbers[n] = 1
```

- `8675309 in list_of_numbers`
  False

- `1240893 in list_of_numbers`
  True

- `8675309 in dict_of_numbers`
  False

- `1240893 in dict_of_numbers`
  True

The `random` module supports a bunch of random number generation operations. We’ll see more on this later in the course. [https://docs.python.org/3/library/random.html](https://docs.python.org/3/library/random.html)
Checking set membership: fast and slow

```python
from random import randint

listlen = 1000000
list_of_numbers = listlen*[0]
dict_of_numbers = dict()

for i in range(listlen):
    n = randint(1000000, 9999999)
    list_of_numbers[i] = n
    dict_of_numbers[n] = 1
```

```
8675309 in list_of_numbers
False

1240893 in list_of_numbers
True

8675309 in dict_of_numbers
False

1240893 in dict_of_numbers
True
```

Initialize a list (of all zeros) and a dictionary.
Checking set membership: fast and slow

```python
from random import randint
listlen = 1000000
list_of_numbers = listlen*[0]
dict_of_numbers = dict()

for i in range(listlen):
    n = randint(1000000, 9999999)
    list_of_numbers[i] = n
    dict_of_numbers[n] = 1
```

Generate `listlen` random numbers, writing them to both the list and the dictionary.

```python
8675309 in list_of_numbers
False

1240893 in list_of_numbers
True

8675309 in dict_of_numbers
False

1240893 in dict_of_numbers
True
```
Checking set membership: fast and slow

```python
from random import randint

listlen = 1000000
list_of_numbers = listlen*[0]
dict_of_numbers = dict()

for i in range(listlen):
    n = randint(1000000, 9999999)
    list_of_numbers[i] = n
    dict_of_numbers[n] = 1
```

This is slow.

<table>
<thead>
<tr>
<th>Number</th>
<th>List Membership</th>
<th>Dictionary Membership</th>
</tr>
</thead>
<tbody>
<tr>
<td>8675309</td>
<td>False</td>
<td>False</td>
</tr>
<tr>
<td>1240893</td>
<td>True</td>
<td>True</td>
</tr>
</tbody>
</table>

This is fast.
Checking set membership: fast and slow

Let's get a more quantitative look at the difference in speed between lists and dicts.

The time module supports accessing the system clock, timing functions, and related operations. [https://docs.python.org/3/library/time.html](https://docs.python.org/3/library/time.html)

Timing parts of your program to find where performance can be improved is called **profiling** your code. Python provides some built-in tools for more profiling, which we'll discuss if time allows. [https://docs.python.org/3/library/profile.html](https://docs.python.org/3/library/profile.html)
Checking set membership: fast and slow

To see how long an operation takes, look at what time it is, perform the operation, and then look at what time it is again. The time difference is how long it took to perform the operation.

```python
import time

start_time = time.time()

8675309 in list_of_numbers

0.10922789573669434
```

Warning: this can be influenced by other processes running on your computer. See documentation for ways to mitigate that inaccuracy.

```python
start_time = time.time()

8675309 in dict_of_numbers

0.0002219676971435547
```
Checking set membership: fast and slow

Checking membership in the dictionary is orders of magnitude faster! Why should that be?
Checking set membership: fast and slow

The time difference is due to how the in operation is implemented for lists and dictionaries. Python compares $x$ against each element in the list until it finds a match or hits the end of the list. So this takes time linear in the length of the list.

Python uses a hash table. For now, it suffices to know that this lets us check if $x$ is in the dictionary in (almost) the same amount of time, regardless of how many items are in the dictionary.
Crash course: hash tables

Let’s say I have a set of 4 items:

I want to find a way to know **quickly** whether or not an item is in this set.
Crash course: hash tables

Hash function maps objects to “buckets”

Let’s say I have a set of 4 items:

- f( red ) = 1
- f( yellow ) = 3
- f( orange ) = 2
- f( green ) = 1

Assign objects to buckets based on the outputs of the hash function.
Crash course: hash tables

Hash function maps objects to “buckets”

Let’s say I have a set of 4 items:

Q: is this item in the set?
Crash course: hash tables

Hash function maps objects to “buckets”

Let’s say I have a set of 4 items:

Q: is this item in the set?

\[ f(\text{item}) = 4 \]

Look in bucket 4. Nothing’s there, so the item wasn’t in the set.
Crash course: hash tables

Hash function maps objects to “buckets”

Let’s say I have a set of 4 items:

Q: is this item in the set?
Crash course: hash tables

Hash function maps objects to “buckets”

Let’s say I have a set of 4 items:

Q: is this item in the set?

\[ f( ) = 2 \]

Look in bucket 2, and we find the object, so it’s in the set.
Crash course: hash tables

Hash function maps objects to “buckets”

Let’s say I have a set of 4 items:

Q: is this item in the set?
Crash course: hash tables

Hash function maps objects to “buckets”

Let’s say I have a set of 4 items:

Q: is this item in the set?

\[ f(\text{item}) = 1 \]

Look in bucket 1, and there’s more than one thing. Compare against each of them, eventually find a match.

When more than one object falls in the same bucket, we call it a hash collision.
Crash course: hash tables

Hash function maps objects to “buckets”

Let’s say I have a set of 4 items:

Q: is this item in the set?
Crash course: hash tables

Hash function maps objects to “buckets”

Let’s say I have a set of 4 items:

Q: is this item in the set?

\[ f(\text{item}) = 1 \]

Look in bucket 1, and there’s more than one thing. Compare against each of them, no match, so it’s not in the set.

Worst possible case: have to check everything in the bucket only to conclude there’s no match.
Crash course: hash tables

Hash function maps objects to “buckets”

**Key point:** hash table lets us avoid comparing against every object in the set (provided we pick a good hash function that has few collisions)

More information:
Downey Chapter B.4
https://en.wikipedia.org/wiki/Hash_table
https://en.wikipedia.org/wiki/Hash_function

For the purposes of this course, it suffices to know that dictionaries (and the related set object, which we'll see soon), have faster membership checking than lists because they use hash tables.
Common pattern: dictionary as counter

Example: counting word frequencies

Naïve idea: keep one variable to keep track of each word
We’re gonna need a lot of variables!

Better idea: use a dictionary, keep track of only the words we see

```python
1  wdcounts = dict()
2  for w in list_of_words:
3    wdcounts[w] += 1
```

This code as written won’t work! It’s your job in one of your homework problems to flesh this out. You may find it useful to read about the `dict.get()` method:

https://docs.python.org/3/library/stdtypes.html#dict.get
Traversing a dictionary

Suppose I have a dictionary representing word counts…

…and now I want to display the counts for each word.

```
for w in wdcnt:
    print(w, wdcnt[w])
```

Traversing a dictionary yields the keys, in no particular order. Typically, you’ll get them in the order they were added, but this is not guaranteed, so don’t rely on it.

This kind of traversal is, once again, a very common pattern when dealing with dictionaries. Dictionaries support iteration over their keys. They, like sequences, are iterators. We’ll see more of this as the course continues.

https://docs.python.org/dev/library/stdtypes.html#iterator-types

(Deconstructed) poem credit: Alfred, Lord Tennyson, *The Charge of the Light Brigade*
Common Pattern: Reverse Lookup and Inversion

Returning to our example, what if I want to map a (real) name to a uniqname? E.g., I want to look up Emmy Noether’s username from her real name.

The keys of `umid2name` are the values of `name2umid` and vice versa. We say that `name2umid` is the reverse lookup table (or the inverse) for `umid2name`.

```python
1 umid2name
2 {'aeinstein': 'Albert Einstein',
3   'cshannon': 'Claude Shannon',
4   'enoether': 'Amalie Emmy Noether',
5   'kyfan': 'Ky Fan'}

1 name2umid = dict()
2 for uname in umid2name:
3   truename = umid2name[uname]
4   name2umid[truename] = uname
5 name2umid

{'Albert Einstein': 'aeinstein',
 'Amalie Emmy Noether': 'enoether',
 'Claude Shannon': 'cshannon',
 'Ky Fan': 'kyfan'}
Common Pattern: Reverse Lookup and Inversion

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```
1 umid2name

{'aeinstein': 'Albert Einstein', 'cshannon': 'Claude Shannon', 'enoether': 'Amalie Emmy Noether', 'kyfan': 'Ky Fan'}
```

The keys of `umid2name` are the values of `name2umid` and vice versa. We say that `name2umid` is the reverse lookup table (or the inverse) for `umid2name`.

```
1 name2umid = dict()
2 for uname in umid2name:
3     truename = umid2name[uname]
4     name2umid[truename] = uname
5 name2umid

{'Albert Einstein': 'aeinstein', 'Amalie Emmy Noether': 'enoether', 'Claude Shannon': 'cshannon', 'Ky Fan': 'kyfan'}
```

What if there are duplicate values? For example, in the word count example, more than one word appears 2 times in the text… How do we deal with that?
Here’s our original word count dictionary (cropped for readability). Some values (e.g., 1 and 3) appear more than once.

Solution: map values with multiple keys to a list of all keys that had that value.

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Here’s our original word count dictionary (cropped for readability). Some values (e.g., 1 and 3) appear more than once.

What if there are duplicate values? For example, in the word count example, more than one word appears 2 times in the text… How do we deal with that?

Solution: map values with multiple keys to a list of all keys that had that value.

Note: there is a more graceful way to do this part of the operation, mentioned in homework 2.
Keys Must be Hashable

```python
1 d = dict()
2 animals = ['cat', 'dog', 'bird', 'goat']
3 d[animals] = 1.61803
```

```
Traceback (most recent call last)
<ipython-input-77-9fa9089d27b7> in <module>(
   1 d = dict()
   2 animals = ['cat', 'dog', 'bird', 'goat']
----> 3 d[animals] = 1.61803

TypeError: unhashable type: 'list'
```

From the documentation: “All of Python’s immutable built-in objects are hashable; mutable containers (such as lists or dictionaries) are not.”
https://docs.python.org/3/glossary.html#term-hashable
Dictionaries can have dictionaries as values!

Suppose I want to map pairs \((x,y)\) to numbers.

```python
1  times_table = dict()
2  for x in range(1,13):
3      if x not in times_table:
4          times_table[x] = dict()
5          for y in range(1,13):
6              times_table[x][y] = x*y
7  times_table[7][9]
```

Each value of \(x\) maps to another dictionary.

Note: We’re putting this if-statement here to illustrate that in practice, we often don’t know the order in which we’re going to observe the objects we want to add to the dictionary.
Dictionaries can have dictionaries as values!

Suppose I want to map pairs (x,y) to numbers.

```python
times_table = dict()
for x in range(1,13):
    if x not in times_table:
        times_table[x] = dict()
    for y in range(1,13):
        times_table[x][y] = x*y
times_table[7][9]
```

Next lecture, we’ll see a more natural way to perform this mapping in particular, but this “dictionary of dictionaries” pattern is common enough that it’s worth seeing.
Common pattern: memoization

```python
def naive_fibo(n):
    if n < 0:
        raise ValueError('Negative Fibonacci number?')
    elif n==0:
        return 0
    elif n==1:
        return 1
    else:
        return naive_fibo(n-1) + naive_fibo(n-2)

for i in range(8,13):
    print(naive_fibo(i))
```

Raise an error. You'll need this in many of your future homeworks. [https://docs.python.org/3/tutorial/errors.html#raising-exceptions](https://docs.python.org/3/tutorial/errors.html#raising-exceptions)
Common pattern: memoization

The inefficiency is clear when we draw the call graph of the function.

We’re doing extra work, computing the same thing over and over. This quickly gets out of hand.
Common pattern: memoization

The inefficiency is clear when we draw the call graph of the function. We're doing extra work, computing the same thing over and over. This quickly gets out of hand.

Solution: store our computations for future reuse. This is called memoization.

We're doing extra work, computing the same thing over and over. This quickly gets out of hand.
Common pattern: memoization

This is the dictionary that we’ll use for memoization. We'll store known[n] = fibo(n) the first time we compute fibo(n), and every time we need it again, we just look it up!

```python
known = {0: 0, 1: 1}
def fibo(n):
    if n in known:
        return known[n]
    else:
        f = fibo(n-1) + fibo(n-2)
        known[n] = f
        return(f)
fibo(30)
```
Common pattern: memoization

```python
known = {0: 0, 1: 1}
def fibo(n):
    if n in known:
        return known[n]
    else:
        f = fibo(n-1) + fibo(n-2)
        known[n] = f
        return(f)

fibo(30)
```

If we already know the n-th Fibonacci number, there's no need to compute it again. Just look it up!
Common pattern: memoization

```python
known = {0: 0, 1: 1}
def fibo(n):
    if n in known:
        return known[n]
    else:
        f = fibo(n-1) + fibo(n-2)
        known[n] = f
        return f
fibo(30)
```

If we don't already know it, we have to compute it, but before we return the result, we memoize it in `known` for future reuse.
Common pattern: memoization

If you try to do this with `naive_fibo`, you’ll be waiting for quite a bit!

The time difference is enormous!

Note: this was done with known set to its initial state, so this is a fair comparison.
Our memoized Fibonacci function can compute some truly huge numbers!

Python runs out of levels of recursion. You can change this maximum recursion depth, but it can introduce instability: https://docs.python.org/3.5/library/sys.html#sys.setrecursionlimit

I cropped some of the error message for readability.
Python runs out of levels of recursion. You can change this maximum recursion depth, but it can introduce instability: https://docs.python.org/3.5/library/sys.html#sys.setrecursionlimit

Our memoized Fibonacci function can compute some truly huge numbers!
Common pattern: memoization

```python
known = {0:0, 1:1}
def fibo(n):
    if n in known:
        return known[n]
    else:
        f = fibo(n-1) + fibo(n-2)
        known[n] = f
        return(f)
fibo(30)
```

Congratulations! You’ve seen your first example of **dynamic programming**! Lots of popular interview questions fall under this purview. E.g., [https://en.wikipedia.org/wiki/Tower_of_Hanoi](https://en.wikipedia.org/wiki/Tower_of_Hanoi)
Common pattern: memoization

```python
1 known = {0:0, 1:1}
2 def fibo(n):
3     if n in known:
4         return known[n]
5     else:
6         f = fibo(n-1) + fibo(n-2)
7         known[n] = f
8         return(f)
9 fibo(30)
```

Note: the dictionary known is declared outside the function fibo. There is a good reason for this: we don’t want known to disappear when we finish running fibo! We say that known is a global variable, because it is defined in the “main” program.
Name Spaces

A **name space** (or **namespace**) is a context in which code is executed.

The “outermost” namespace (also called a **frame**) is called `__main__`

Running from the command line or in Jupyter? You’re in `__main__`

Often shows up in error messages, something like,

> “Error ... in `__main__`: blah blah blah”

Variables defined in `__main__` are said to be **global**

Function definitions create their own **local** namespaces

Variables defined in such a context are called **local**

Local variables cannot be accessed from outside their frame/namespace

Similar behavior inside for-loops, while-loops, etc
Name Spaces

Example: we have a program simulating a light bulb
Bulb state is represented by a global Boolean variable, `lightbulb_on`

```python
1 lightbulb_on = False
2 def lights_on():
3     lightbulb_on = True
4     lights_on()
5 lightbulb_on
```

But after calling `lights_on`, the state variable is still `False`. What’s going on?
Name Spaces

The fact that this code causes an error shows what is really at issue. By default, Python treats the variable `lightbulb_on` inside the function definition as being a different variable from the `lightbulb_on` defined in the main namespace. This is, generally, a good design. It prevents accidentally changing global state information.
Name Spaces

We have to tell Python that we want `lightbulb_on` to mean the `global` variable of the same name.

```python
lightbulb_on = False
def flip_switch():
    global lightbulb_on
    lightbulb_on = not lightbulb_on
flip_switch()
lightbulb_on
```

```
True
```

```python
flip_switch()
lightbulb_on
```

```
False
```

**Warning:** this is all well and good, but it is considered best practice to avoid global variables in large programs, as they can make debugging hard. This isn’t so crucial for our course, since we won’t be building anything especially large, but you should be aware of it.
Readings (this lecture)

Required:
- Downey Chapter 11 or Severance Chapter 9

Recommended:
- Downey Chapter B.4
- Python documentation on dictionaries
  - https://docs.python.org/3/tutorial/datastructures.html#dictionaries
  - https://docs.python.org/3/library/stdtypes.html#mapping-types-dict
Readings (next lecture)

Required:
  Downey Chapter 12 or Severance Chapter 10

Recommended:
  Downey Chapter 13
  Python documentation on tuples
    https://docs.python.org/3/library/stdtypes.html#tuples
    https://docs.python.org/3/tutorial/datastructures.html#tuples-and-sequences