## STAT371

## DISCUSSION 2

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TA: Ruiyan Luo Office: 4268 CSSC

Office hours: TW 2:30–3:30pm Phone number: 262-8182 E-mail: rluo@stat.wisc.edu

## 1. Measures of center:

• sample mean  $(\bar{y})$ :

$$\bar{y} = \frac{\sum y_i}{n}$$

where the  $y_i$ 's are the observations in the sample and n is the sample size (that is, the number of  $y_i$ 's). Mean is sensitive to outlying values.

• median:

the value that mostly nearly lies in the middle of the sample. For orderded values, when sample size is odd, median=the value for the middle observation; when sample size is even, median = the average of the middle two.

## 2. Boxplot

• quartiles:

The median splits the distribution into two parts. The first quartile  $(Q_1)$ , is the median of the data values in the lower half of the data set. The third quartile  $(Q_3)$ , is the median of the data values in the upper half of the data set.

A common alternative definition for quartiles is:  $Q_1$  has rank position (.25)(n+1) and  $Q_3$  has rank position (.75)(n+1). Interquartile range (IQR): IQR=  $Q_3 - Q_1$ 

• boxplot: a visual representation of the five-number summary: the minumum, the maximum, the median and the quartiles. Note: The scale on the numeric axis should consistent without breaks and with the same scale throughout.

• outliers:

lower fence = 
$$Q_1 - 1.5 \times IQR$$
  
upper fence =  $Q_3 + 1.5 \times IQR$ 

An outlier is a data point that falls outside of the fences.

- parallel boxplot and modified boxplot
- 3. Measures of Dispersion
  - $\bullet\,$  the range=mazimum-minumum
  - deviation=observation- $\bar{y}$
  - the standard deviation (s):

$$s = \sqrt{\frac{\sum (y_i - \bar{y})^2}{n - 1}}$$

In this formula, the expression  $\sum (y_i - \bar{y})^2$  denotes the sum of the squared deviations.

- variance  $(s^2)$ : the squared standard deviation.
- $\bullet$  the coefficient of variation= $\!\frac{s}{\bar{y}}\times 100\%$